

Note: For the benefit of the students, specially the aspiring ones, the question of JEE(advanced), 2022 are also given in this booklet. Keeping the interest of students studying in class XI, the questions based on topics from class XI have been marked with ‘*’, which can be attempted as a test. For this test the time allocated in Mathematics, Physics and Chemistry are 30 minutes, 20 minutes and 25 minutes respectively.

FIITJEE

SOLUTIONS TO JEE (ADVANCED) – 2022 (PAPER-2)

MATHEMATICS

SECTION 1 (Maximum marks : 24)

- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER ranging from 0 to 9, BOTH INCLUSIVE.**
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designed to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:

Full Mark	:	+3	If ONLY the correct integer is entered;
Zero Marks	:	0	If the question is unanswered;
Negative Marks	:	-1	In all other cases.

- *Q. 1. Let α and β be real numbers such that $-\frac{\pi}{4} < \beta < 0 < \alpha < \frac{\pi}{4}$. If $\sin(\alpha + \beta) = \frac{1}{3}$ and $\cos(\alpha - \beta) = \frac{2}{3}$, then the greatest integer less than or equal to $\left(\frac{\sin \alpha}{\cos \beta} + \frac{\cos \beta}{\sin \alpha} + \frac{\cos \alpha}{\sin \beta} + \frac{\sin \beta}{\cos \alpha}\right)^2$ is _____.
- Q. 2. If $y(x)$ is the solution of the differential equation $x dy - (y^2 - 4y) dx = 0$ for $x > 0$, $y(1) = 2$, and the slope of the curve $y = y(x)$ is never zero, then the value of $10y(\sqrt{2})$ is _____.
- Q.3. The greatest integer less than or equal to $\int_1^2 \log_2(x^3 + 1) dx + \int_1^{\log_2 9} (2^x - 1)^{1/3} dx$ is _____.
- *Q.4. The product of all positive real values of x satisfying the equation $x^{(16(\log_5 x)^3 - 68 \log_5 x)} = 5^{-16}$ is _____.
- Q.5. If $\beta = \lim_{x \rightarrow 0} \frac{e^{x^3} - (1 - x^3)^{1/3} + ((1 - x^2)^{1/2} - 1) \sin x}{x \sin^2 x}$, then the value of 6β is _____.

Q.6. Let β be real number. Consider the matrix $A = \begin{pmatrix} \beta & 0 & 1 \\ 2 & 1 & -2 \\ 3 & 1 & -2 \end{pmatrix}$. If $A^7 - (\beta - 1)A^6 - \beta A^5$ is a singular matrix,

then the value of 9β is _____.

*Q.7. Consider the hyperbola $\frac{x^2}{100} - \frac{y^2}{64} = 1$ with foci at S and S_1 , where S lies on the positive x-axis. Let P be a point on the hyperbola, in the first quadrant. Let $\angle SPS_1 = \alpha$, with $\alpha < \frac{\pi}{2}$. The straight line passing through the point S and having the same slope as that of the tangent at P to the hyperbola, intersects the straight line S_1P at P_1 . Let δ be the distance of P from the straight line SP_1 , and $\beta = S_1P$. Then the greatest integer less than or equal to $\frac{\beta\delta}{9} \sin \frac{\alpha}{2}$ is _____.

Q.8. Consider the function $f, g : \mathbb{R} \rightarrow \mathbb{R}$ defined by $f(x) = x^2 + \frac{5}{12}$ and $g(x) = \begin{cases} 2\left(1 - \frac{4|x|}{3}\right), & |x| \leq \frac{3}{4}, \\ 0, & |x| > \frac{3}{4}. \end{cases}$. If α is

the area of the region $\left\{ (x, y) \in \mathbb{R} \times \mathbb{R} : |x| \leq \frac{3}{4}, 0 \leq y \leq \min\{f(x), g(x)\} \right\}$, then the value of 9α is _____.

SECTION 2 (Maximum marks: 24)

- This section contains **SIX (06)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONE OR MORE THAN ONE** of these four option(s) is (are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
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<i>Full Mark</i>	:	+4	ONLY If (all) the correct option(s) is(are) chosen;
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<i>Zero Marks</i>	:	0	If unanswered;
<i>Negative Marks</i>	:	-2	In all other cases.

*Q.9. Let PQRS be a quadrilateral in a plane, where $QR = 1$, $\angle PQR = \angle QRS = 70^\circ$, $\angle PQS = 15^\circ$ and $\angle PRS = 40^\circ$. If $\angle RPS = \theta^\circ$, $PQ = \alpha$ and $PS = \beta$, then the interval(s) that contain(s) the value of $4\alpha\beta \sin\theta^\circ$ is/are

- (A) $(0, \sqrt{2})$ (B) $(1, 2)$
 (C) $(\sqrt{2}, 3)$ (D) $(2\sqrt{2}, 3\sqrt{2})$

Q.10. Let $\alpha = \sum_{k=1}^{\infty} \sin^{2k} \left(\frac{\pi}{6} \right)$. Let $g : [0, 1] \rightarrow \mathbb{R}$ be the function defined by $g(x) = 2^{\alpha x} + 2^{\alpha(1-x)}$. Then, which of the following statements is/are TRUE?

- (A) The minimum value of $g(x)$ is $2^{\frac{7}{6}}$

- (B) The maximum value of $g(x)$ is $1 + 2^{\frac{1}{3}}$
- (C) The function $g(x)$ attains its maximum at more than one point
- (D) The function $g(x)$ attains its minimum at more than one point

*Q.11. Let \bar{z} denote the complex conjugate of a complex number z . If z is a non-zero complex number for which both real and imaginary parts of $(\bar{z})^2 + \frac{1}{z^2}$ are integers, then which of the following is/are possible value(s) of $|z|$?

- (A) $\left(\frac{43 + 3\sqrt{205}}{2}\right)^{\frac{1}{4}}$
- (B) $\left(\frac{7 + \sqrt{33}}{4}\right)^{\frac{1}{4}}$
- (C) $\left(\frac{9 + \sqrt{65}}{4}\right)^{\frac{1}{4}}$
- (D) $\left(\frac{7 + \sqrt{13}}{6}\right)^{\frac{1}{4}}$

*Q.12. Let G be a circle of radius $R > 0$. Let G_1, G_2, \dots, G_n be n circles of equal radius $r > 0$. Suppose each of the n circles G_1, G_2, \dots, G_n touches the circle G externally. Also, for $i = 1, 2, \dots, n - 1$, the circle G_i touches G_{i+1} externally, and G_n touches G_1 externally. Then, which of the following statements is/are TRUE?

- (A) If $n = 4$, then $(\sqrt{2} - 1)r < R$
- (B) If $n = 5$, then $r < R$
- (C) If $n = 8$, then $(\sqrt{2} - 1)r < R$
- (D) If $n = 12$, then $\sqrt{2}(\sqrt{3} + 1)r > R$.

Q.13. Let \hat{i}, \hat{j} and \hat{k} be the unit vectors along the three positive coordinate axes. Let

$$\vec{a} = 3\hat{i} + \hat{j} - \hat{k},$$

$$\vec{b} = \hat{i} + b_2\hat{j} + b_3\hat{k}, \quad b_2, b_3 \in \mathbb{R}$$

$$\vec{c} = c_1\hat{i} + c_2\hat{j} + c_3\hat{k}, \quad c_1, c_2, c_3 \in \mathbb{R}$$

be the vectors such that $b_2 b_3 > 0$, $\vec{a} \cdot \vec{b} = 0$ and

$$\begin{pmatrix} 0 & -c_3 & c_2 \\ c_3 & 0 & -c_1 \\ -c_2 & c_1 & 0 \end{pmatrix} \begin{pmatrix} 1 \\ b_2 \\ b_3 \end{pmatrix} = \begin{pmatrix} 3 - c_1 \\ 1 - c_2 \\ -1 - c_3 \end{pmatrix}$$

Then, which of the following is/are TRUE?

- (A) $\vec{a} \cdot \vec{c} = 0$
- (B) $\vec{b} \cdot \vec{c} = 0$
- (C) $|\vec{b}| > \sqrt{10}$
- (D) $|\vec{c}| \leq \sqrt{11}$.

Q.14. For $x \in \mathbb{R}$, let the function $y(x)$ be the solution of the differential equation

$$\frac{dy}{dx} + 12y = \cos\left(\frac{\pi}{12}x\right), \quad y(0) = 0.$$

Then, which of the following statements is/are TRUE?

- (A) $y(x)$ is an increasing function
- (B) $y(x)$ is a decreasing function
- (C) There exists a real number β such that the line $y = \beta$ intersects the curve $y = y(x)$ at infinitely many points
- (D) $y(x)$ is a periodic function

SECTION 3 (Maximum marks: 12)

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- *Q.15. Consider 4 boxes, where each box contains 3 red balls and 2 blue balls. Assume that all 20 balls are distinct. In how many different ways can 10 balls be chosen from these 4 boxes so that from each box at least one red ball and one blue ball are chosen?
- (A) 21816 (B) 85536
 (C) 12096 (D) 156816

- Q.16. If $M = \begin{pmatrix} \frac{5}{2} & \frac{3}{2} \\ -\frac{3}{2} & -\frac{1}{2} \end{pmatrix}$, then which of the following matrices is equal to M^{2022} ?
- (A) $\begin{pmatrix} 3034 & 3033 \\ -3033 & -3032 \end{pmatrix}$ (B) $\begin{pmatrix} 3034 & -3033 \\ 3033 & -3032 \end{pmatrix}$
 (C) $\begin{pmatrix} 3033 & 3032 \\ -3032 & -3031 \end{pmatrix}$ (D) $\begin{pmatrix} 3032 & 3031 \\ -3031 & -3030 \end{pmatrix}$

- Q.17. Suppose that
 Box-I contains 8 red, 3 blue and 5 green balls,
 Box-II contains 24 red, 9 blue and 15 green balls,
 Box-III contains 1 blue, 12 green and 3 yellow balls,
 Box-IV contains 10 green, 16 orange and 6 white balls,
 A ball is chosen randomly for Box-I; call that ball b. If b is red then a ball is chosen randomly from Box-II, if b is blue then a ball is chosen randomly from Box-III, and if b is green then a ball is chosen randomly from Box-IV. The conditional probability of the event 'one of the chosen balls is white' given that the event 'at least one of the chosen ball is green' has happened, is equal to
- (A) $\frac{15}{256}$ (B) $\frac{3}{16}$
 (C) $\frac{5}{52}$ (D) $\frac{1}{8}$

- Q.18. For positive integer n, define
- $$f(n) = n + \frac{16 + 5n - 3n^2}{4n + 3n^2} + \frac{32 + n - 3n^2}{8n + 3n^2} + \frac{48 - 3n - 3n^2}{12n + 3n^2} + \dots + \frac{25n - 7n^2}{7n^2}.$$
- Then, the value of $\lim_{n \rightarrow \infty} f(n)$ is equal to
- (A) $3 + \frac{4}{3} \log_e 7$ (B) $4 - \frac{3}{4} \log_e \left(\frac{7}{3}\right)$
 (C) $4 - \frac{4}{3} \log_e \left(\frac{7}{3}\right)$ (D) $3 + \frac{3}{4} \log_e 7.$

PHYSICS

SECTION 1 (Maximum marks : 24)

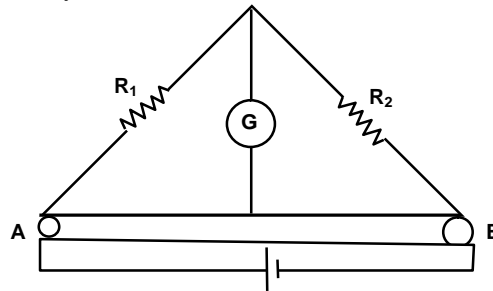
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*Q.1 A particle of mass 1 kg is subjected to a force which depends on the position as $\vec{F} = -k(x\hat{i} + y\hat{j})$ kg ms⁻² with $k = 1$ kg s⁻². At time $t = 0$, the particle's position $\vec{r} = \left(\frac{1}{\sqrt{2}}\hat{i} + \sqrt{2}\hat{j}\right)$ m and its velocity $\vec{v} = \left(-\sqrt{2}\hat{i} + \sqrt{2}\hat{j} + \frac{2}{\pi}\hat{k}\right)$ ms⁻¹. Let v_x and v_y denote the x and the y components of the particle's velocity, respectively. **Ignore gravity**. When $z = 0.5$ m, the value of $(x v_y - y v_x)$ is _____ m² s⁻¹.

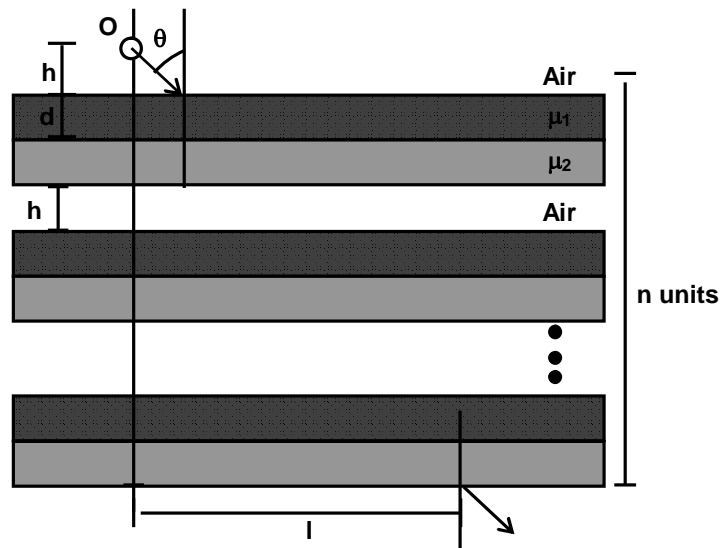
Q.2 In a radioactive decay chain reaction, ${}_{90}^{230}\text{Th}$ nucleus decays into ${}_{84}^{214}\text{Po}$ nucleus. The ratio of the number of α to number of β^- particles emitted in this process is _____

Q.3 Two resistances $R_1 = X \Omega$ and $R_2 = 1 \Omega$ are connected to a wire AB of uniform resistivity, as shown in the figure. The radius of the wire varies linearly along its axis from 0.2mm at A to 1mm at B. A galvanometer (G) connected to the center of the wire, 50cm from each end along its axis, shows zero deflection when A and B are connected to a battery. The value of X is _____

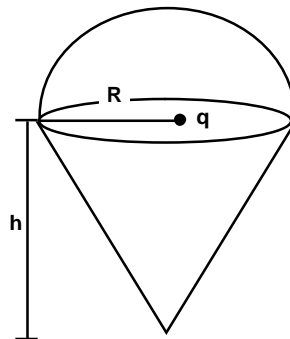


Q.4 In a particular system of units, a physical quantity can be expressed in terms of the electric charge e , electron mass m_e , Planck's constant h , and Coulomb's constant $k = \frac{1}{4\pi\epsilon_0}$, where ϵ_0 is the permittivity of vacuum. In terms of these physical constants, the dimension of the magnetic field is $[B] = [e]^\alpha [m_e]^\beta [h]^\gamma [k]^\delta$. The value of $\alpha + \beta + \gamma + \delta$ is _____.

- Q.5 Consider a configuration of n identical units, each consisting of three layers. The first layer is a column of air of height $h = \frac{1}{3}$ cm, and the second and third layers are of equal thickness $d = \frac{\sqrt{3}-1}{2}$ cm, and refractive indices $\mu_1 = \sqrt{\frac{3}{2}}$ and $\mu_2 = \sqrt{3}$, respectively. A light source O is placed on the top of the first unit, as shown in the figure. A ray of light from O is incident on the second layer of the first unit at an angle of $\theta = 60^\circ$ to the normal. For a specific value of n , the ray of light emerges from the bottom of the configuration at a distance $l = \frac{8}{\sqrt{3}}$ cm, as shown in the figure. The value of n is _____.

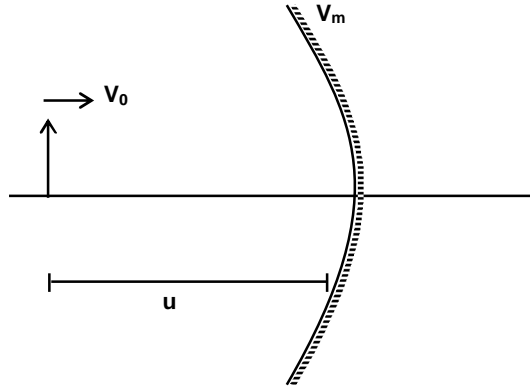


- Q.6 A charge q is surrounded by a closed surface consisting of an inverted cone of height h and base radius R , and a hemisphere of radius R as shown in the figure. The electric flux through the conical surface is $\frac{nq}{6\epsilon_0}$ (in SI units). The value of n is _____



- *Q.7 On a frictionless horizontal plane, a bob of mass $m = 0.1$ kg is attached to a spring with natural length $l_0 = 0.1$ m. The spring constant is $k_1 = 0.009 \text{ Nm}^{-1}$ when the length of the spring $l > l_0$ and is $k_2 = 0.016 \text{ Nm}^{-1}$ when $l < l_0$. Initially the bob is released from $l = 0.15$ m. Assume that Hooke's law remains valid throughout the motion. If the time period of the full oscillation is $T = (n\pi)$ s, then the integer closest to n is _____

- Q.8 An object and a concave mirror of focal length $f=10\text{cm}$ both move along the principal axis of the mirror with constant speeds. The object moves with speed $V_0=15\text{ cm s}^{-1}$ towards the mirror with respect to a laboratory frame. The distance between the object and the mirror at a given moment is denoted by u . When $u=30\text{ cm}$, the speed of the mirror V_m is such that the image is instantaneously at rest with respect to the laboratory frame, and the object forms a real image. The magnitude of V_m is _____ cm s^{-1}

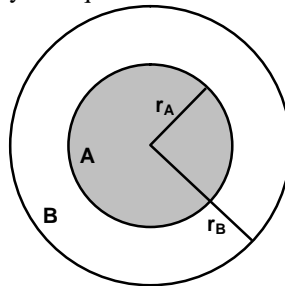


SECTION 2 (Maximum marks: 24)

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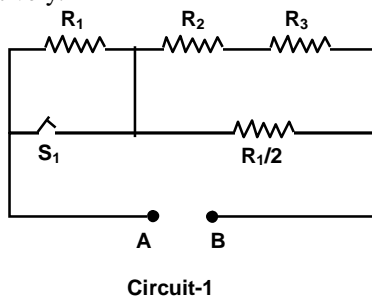
- Q.9 In the figure, the inner (shaded) region A represents a sphere of radius $r_A=1$, within which the electrostatic charge density varies with the radial distance r from the center as $\rho_A=kr$, where k is positive. In the spherical shell B of outer radius r_B , the electrostatic charge density varies as $\rho_B = \frac{2k}{r}$. Assume that dimensions are taken care of. All physical quantities are in their SI units.



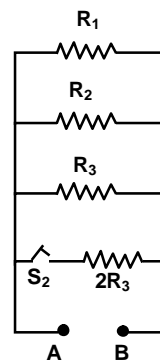
Which of the following statement(s) is(are) correct?

- (A) If $r_B = \sqrt{\frac{3}{2}}$, then the electric field is zero everywhere outside B .
 (B) If $r_B = \frac{3}{2}$, then the electric potential just outside B is $\frac{k}{\epsilon_0}$.
 (C) If $r_B = 2$, then the total charge of the configuration is $15\pi k$.
 (D) If $r_B = \frac{5}{2}$, then the magnitude of the electric field just outside B is $\frac{13\pi k}{\epsilon_0}$.

- Q.10 In Circuit-1 and Circuit-2 shown in the figures, $R_1 = 1 \Omega$, $R_2 = 2 \Omega$ and $R_3 = 3 \Omega$. P_1 and P_2 are the power dissipations in Circuit-1 and Circuit-2 when the switches S_1 and S_2 are in open conditions, respectively.
 Q_1 and Q_2 are the power dissipations in Circuit-1 and Circuit-2 when the switches S_1 and S_2 are in closed conditions, respectively.



Circuit-1



Circuit-2

Which of the following statement(s) is(are) correct?

- (A) When a voltage source of 6 V is connected across A and B in both circuits, $P_1 < P_2$.
 (B) When a constant current source of 2 Amp is connected across A and B in both circuits, $P_1 > P_2$.
 (C) When a voltage source of 6 V is connected across A and B in Circuit-1, $Q_1 > P_1$.
 (D) When a constant current source of 2 Amp is connected across A and B in both circuits, $Q_2 < Q_1$.
- *Q.11 A bubble has surface tension S . The ideal gas inside the bubble has ratio of specific heats $\gamma = \frac{5}{3}$. The

bubble is exposed to the atmosphere and it always retains its spherical shape. When the atmospheric pressure is P_{a1} , the radius of the bubble is found to be r_1 and the temperature of the enclosed gas is T_1 . When the atmospheric pressure is P_{a2} , the radius of the bubble and the temperature of the enclosed gas are r_2 and T_2 , respectively.

Which of the following statement(s) is(are) correct?

- (A) If the surface of the bubble is a perfect heat insulator, then $\left(\frac{r_1}{r_2}\right)^5 = \frac{P_{a2} + \frac{2S}{r_2}}{P_{a1} + \frac{2S}{r_1}}$
 (B) If the surface of the bubble is a perfect heat insulator, then the total internal energy of the bubble including its surface energy does not change with the external atmospheric pressure.
 (C) If the surface of the bubble is a perfect heat conductor and the change in atmospheric temperature is

negligible, then $\left(\frac{r_1}{r_2}\right)^3 = \frac{P_{a2} + \frac{4S}{r_2}}{P_{a1} + \frac{4S}{r_1}}$

(D) If the surface of the bubble is a perfect heat insulator, then $\left(\frac{T_2}{T_1}\right)^{\frac{5}{2}} = \frac{P_{\alpha 2} + \frac{4S}{r_2}}{P_{\alpha 1} + \frac{4S}{r_1}}$

Q12. A disk of radius R with uniform positive charge density σ is placed on the xy plane with its centre at the origin. The Coulomb potential along the z -axis is

$$V(z) = \frac{\sigma}{2\epsilon_0} \left(\sqrt{R^2 + z^2} - z \right).$$

A particle of positive charge q is placed initially at rest at a point on the z axis with $z = z_0$ and $z_0 > 0$. In addition to the Coulomb force, the particle experiences a vertical force $\vec{F} = -c\hat{k}$ with $c > 0$. Let

$\beta = \frac{2c\epsilon_0}{q\sigma}$. Which of the following statements(s) is (are) correct?

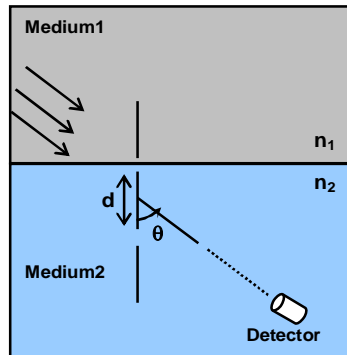
(A) For $\beta = \frac{1}{4}$ and $z_0 = \frac{25}{7}R$, the particle reaches the origin.

(B) For $\beta = \frac{1}{4}$ and $z_0 = \frac{3}{7}R$, the particle reaches the origin.

(C) For $\beta = \frac{1}{4}$ and $z_0 = \frac{R}{\sqrt{3}}$, the particle returns back to $z=z_0$.

(D) For $\beta > 1$ and $z_0 > 0$, the particle always reaches the origin.

Q.13 A double slit setup is shown in the figure. One of the slits is in medium 2 of refractive index n_2 . The other slit is at the interface of this medium with another medium 1 of refractive index $n_1 (\neq n_2)$. The line joining the slits is perpendicular to the interface and the distance between the slits is d . The slit widths are much smaller than d . A monochromatic parallel beam of light is incident on the slits from medium 1. A detector is placed in medium 2 at a large distance from the slits, and at an angle θ from the line joining them, so that θ equals the angle of refraction of the beam. Consider two approximately parallel rays from the slits received by the detector.



Which of the following statement(s) is(are) correct?

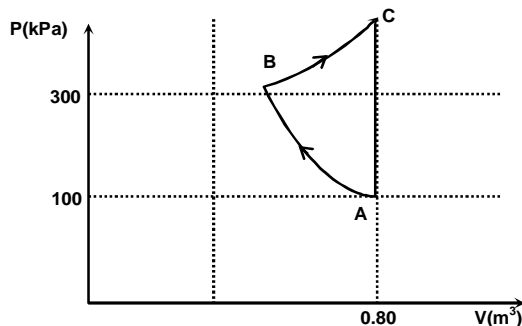
(A) The phase difference between the two rays is independent of d .

(B) The two rays interfere constructively at the detector.

(C) The phase difference between the two rays depends on n_1 but is independent of n_2 .

(D) The phase difference between the two rays vanishes only for certain values of d and the angle of incidence of the beam, with θ being the corresponding angle of refraction.

- *Q.14 In the given P-V diagram, a monoatomic gas ($\gamma = \frac{5}{3}$) is first compressed adiabatically from state A to state B. Then it expands isothermally from state B to state C. [Given : $(\frac{1}{3})^{0.6} \approx 0.5$, $\ln 2 \approx 0.7$].



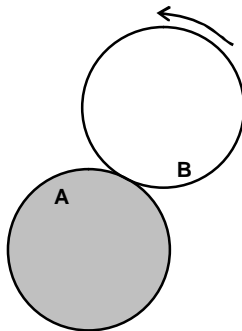
Which of the following statement(s) is(are) correct?

- (A) The magnitude of the total work done in the process $A \rightarrow B \rightarrow C$ is 144kJ .
 (B) The magnitude of the work done in the process $B \rightarrow C$ is 84kJ .
 (C) The magnitude of the work done in the process $A \rightarrow B$ is 60kJ .
 (D) The magnitude of the work done in the process $C \rightarrow A$ is zero.

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- *Q.15 A flat surface of a thin uniform disk A of radius R is glued to a horizontal table. Another thin uniform disk B of mass M and with the same radius R rolls without slipping on the circumference of A, as shown in the figure. A flat surface of B also lies on the plane of the table. The center of mass of B has fixed angular speed ω about the vertical axis passing through the center of A. The angular momentum of B is $nM\omega R^2$ with respect to the center of A. Which of the following is the value of n ?



- (A) 2 (B) 5 (C) 7/2 (D) 9/2

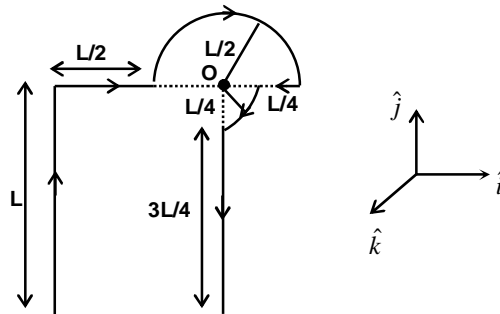
- Q.16 When light of a given wavelength is incident on a metallic surface, the minimum potential needed to stop the emitted photoelectrons is 6.0V . This potential drops to 0.6V if another source with wavelength four times that of the first one and intensity half of the first one is used. What are the wavelength of the first source and the work function of the metal, respectively? [Take $hc/e = 1.24 \times 10^{-6} \text{JmC}^{-1}$.]
- (A) $1.72 \times 10^{-7} \text{m}$, 1.20eV
 (B) $1.72 \times 10^{-7} \text{m}$, 5.60eV
 (C) $3.78 \times 10^{-7} \text{m}$, 5.60eV
 (D) $3.78 \times 10^{-7} \text{m}$, 1.20eV

- Q.17 Area of the cross-section of a wire is measured using a screw gauge. The pitch of the main scale is 0.5mm . The circular scale has 100 divisions and for one full rotation of the circular scale, the main scale shifts by two divisions. The measured readings are listed below.

Measurement condition	Main scale reading	Circular scale reading
Two arms of gauge touching each other without wire	0 division	4 divisions
Attempt-1 : With wire	4 divisions	20 divisions
Attempt-2 : With wire	4 divisions	16 divisions

What are the diameter and cross-sectional area of the wire measured using the screw gauge?

- (A) $2.22 \pm 0.02\text{mm}$, $\pi(1.23 \pm 0.02)\text{mm}^2$
 (B) $2.22 \pm 0.01\text{mm}$, $\pi(1.23 \pm 0.01)\text{mm}^2$
 (C) $2.14 \pm 0.02\text{mm}$, $\pi(1.14 \pm 0.02)\text{mm}^2$
 (D) $2.14 \pm 0.01\text{mm}$, $\pi(1.14 \pm 0.01)\text{mm}^2$
18. Which one of the following options represents the magnetic field \vec{B} at O due to the current flowing in the given wire segments lying on the xy plane?



- (A) $\vec{B} = \frac{-\mu_0 I}{L} \left(\frac{3}{2} + \frac{1}{4\sqrt{2}\pi} \right) \hat{k}$
 (B) $\vec{B} = -\frac{\mu_0 I}{L} \left(\frac{3}{2} + \frac{1}{2\sqrt{2}\pi} \right) \hat{k}$
 (C) $\vec{B} = \frac{-\mu_0 I}{L} \left(1 + \frac{1}{4\sqrt{2}\pi} \right) \hat{k}$
 (D) $\vec{B} = \frac{-\mu_0 I}{L} \left(1 + \frac{1}{4\pi} \right) \hat{k}$

CHEMISTRY

SECTION 1 (Maximum Marks: 24)

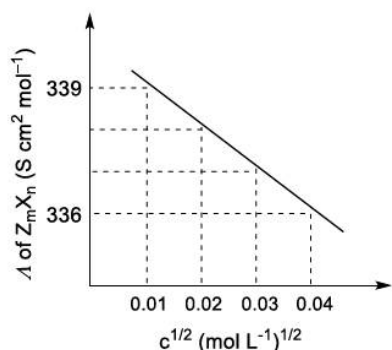
- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER ranging from 0 TO 9, BOTH INCLUSIVE**.
- For each question, enter the correct integer corresponding to the answer using the using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:
Full Marks : +3 If **ONLY** the correct integer is entered;
Zero Marks : 0 If the question is unanswered;
Negative Marks : -1 In all other cases.

- *Q. 1 Concentration of H_2SO_4 and Na_2SO_4 in a solution is 1 M and 1.8×10^{-2} M, respectively. Molar solubility of PbSO_4 in the same solution is $X \times 10^{-Y}$ M (expressed in scientific notation). The value of Y is_____.
- [Given : Solubility product of PbSO_4 (K_{sp}) = 1.6×10^{-8} . For H_2SO_4 , K_{a_1} is very large and $K_{a_2} = 1.2 \times 10^{-2}$]
- Q. 2 An aqueous solution is prepared by dissolving 0.1 mol of an ionic salt in 1.8 kg of water at 35°C . The salt remains 90% dissociated in the solution. The vapour pressure of the solution is 59.724 mm of Hg. Vapor pressure of water at 35°C is 60.000 mm of Hg. The number of ions present per formula unit of the ionic salt is_____.
- Q. 3 Consider the strong electrolytes $Z_m X_n$, $U_m Y_p$ and $V_m X_n$. Limiting molar conductivity (Λ^0) of $U_m Y_p$ and $V_m X_n$ are 250 and 440 $\text{S cm}^2 \text{ mol}^{-1}$, respectively. The value of $(m + n + p)$ is_____.
- Given:

Ion	Z^{n+}	U^{p+}	V^{n+}	X^{m-}	Y^{m-}
λ^0 ($\text{S cm}^2 \text{ mol}^{-1}$)	50.0	25.0	100.0	80.0	100.0

λ^0 is the limiting molar conductivity of ions.

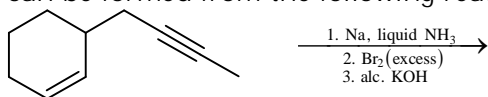
The plot of molar conductivity (Λ) of $Z_m X_n$ vs $c^{1/2}$ is given below.



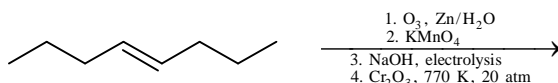
- Q. 4 The reaction of Xe and O_2F_2 gives a Xe compound **P**. The number of moles of HF produced by the complete hydrolysis of 1 mol of **P** is_____.

*Q. 5 Thermal decomposition of AgNO_3 produces two paramagnetic gases. The total number of electrons present in the antibonding molecular orbitals of the gas that has the higher number of unpaired electrons is_____.

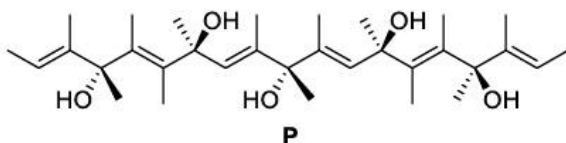
*Q. 6 The number of isomeric tetraenes (**NOT** containing sp -hybridized carbon atoms) that can be formed from the following reaction sequence is_____.



*Q. 7 The of $-\text{CH}_2-$ (methylene) groups in the product formed from the following reaction sequence is_____.



*Q. 8 The total number of chiral molecules formed from one molecule of **P** on complete ozonolysis ($\text{O}_3, \text{Zn/H}_2\text{O}$) is_____.



SECTION 2 (Maximum Marks: 24)

This section contains **SIX (06)** questions.

• Each question has **FOUR** options (A), (B), (C) and (D). **ONE OR MORE THAN ONE** of these four option(s) is (are) correct answer(s).

• For each question, choose the option(s) corresponding to (all) the correct answer(s).

• Answer to each question will be evaluated according to the following marking scheme:

Full Marks : +4 **ONLY** if (all) the correct option(s) is (are) chosen;

Partial Marks : +3 If all the four options are correct but **ONLY** three options are chosen;

Partial Marks : +2 If three or more options are correct but **ONLY** two options are chosen, both of which are correct;

Partial Marks : +1 If two or more options are correct but **ONLY** one option is chosen and it is a correct option;

Zero Marks : 0 If unanswered;

Negative Marks : -2 In all other cases.

*Q.9. To check the principle of multiple proportions, a series of pure binary compounds (P_mQ_n) were analyzed and their composition is tabulated below. The correct option(s) is(are)

Compound	Weight % of P	Weight % of Q
1	50	50
2	44.4	55.6
3	40	60

(A) If empirical formula of compound **3** is P_3Q_4 , then the empirical formula of compound **2** is P_3Q_5 .

(B) If empirical formula of compound **3** is P_3Q_2 , and atomic weight of element P is 20, then the atomic weight of Q is 45.

(C) If empirical formula of compound **2** is PQ , then the empirical formula of compound **1** is P_5Q_4 .

(D) If atomic weight of P and Q are 70 and 35, respectively, then the empirical formula of compound **1** is P_2Q .

Q. 10 The correct option(s) about entropy (S) is(are)
[R = gas constant, F = Faraday constant, T = Temperature]

- (A) For the reaction, $M(s) + 2H^+(aq) \longrightarrow H_2(g) + M^{2+}(aq)$, if $\frac{dE_{\text{cell}}}{dT} = \frac{R}{F}$, then the entropy change of the reaction is R (assume that entropy and internal energy changes are temperature independent).
- (B) The cell reaction, $Pt(s) | H_2(g, 1 \text{ bar}) | H^+(aq, 0.01 \text{ M}) || H^+(aq, 0.1 \text{ M}) | H_2(g, 1 \text{ bar}) | Pt(s)$, is in an entropy driven process.
- (C) For racemisation of an optically active compound, $\Delta S > 0$.
- (D) $\Delta S > 0$, for $[Ni(H_2O)_6]^{2+} + 3 \text{ en} \longrightarrow [Ni(en)_3]^{2+} + 6H_2O$ (where en = ethylenediamine).

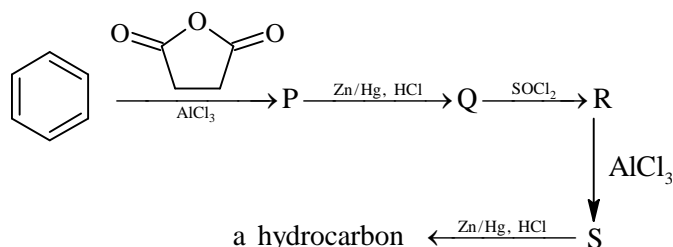
*Q. 11 The compound(s) which react(s) with NH_3 to give boron nitride (BN) is(are)

- (A) B (B) B_2H_6
(C) B_2O_3 (D) BF_4

Q. 12 The correct option(s) related to the extraction of iron from its ore in the blast furnace operating in the temperature range 900 – 1500 K is(are)

- (A) Limestone is used to remove silicate impurity.
(B) Pig iron obtained from blast furnace contains about 4% carbon.
(C) Coke (C) converts CO_2 to CO.
(D) Exhaust gases consist of NO_2 and CO.

*Q. 13 Considering the following reaction sequence, the correct statement(s) is(are)



- (A) Compound **P** and **Q** are carboxylic acids.
(B) Compound **S** decolorizes bromine water.
(C) Compounds **P** and **S** react with hydroxylamine to give the corresponding oximes.
(D) Compound **R** reacts with dialkylcadmium to give the corresponding tertiary alcohol.

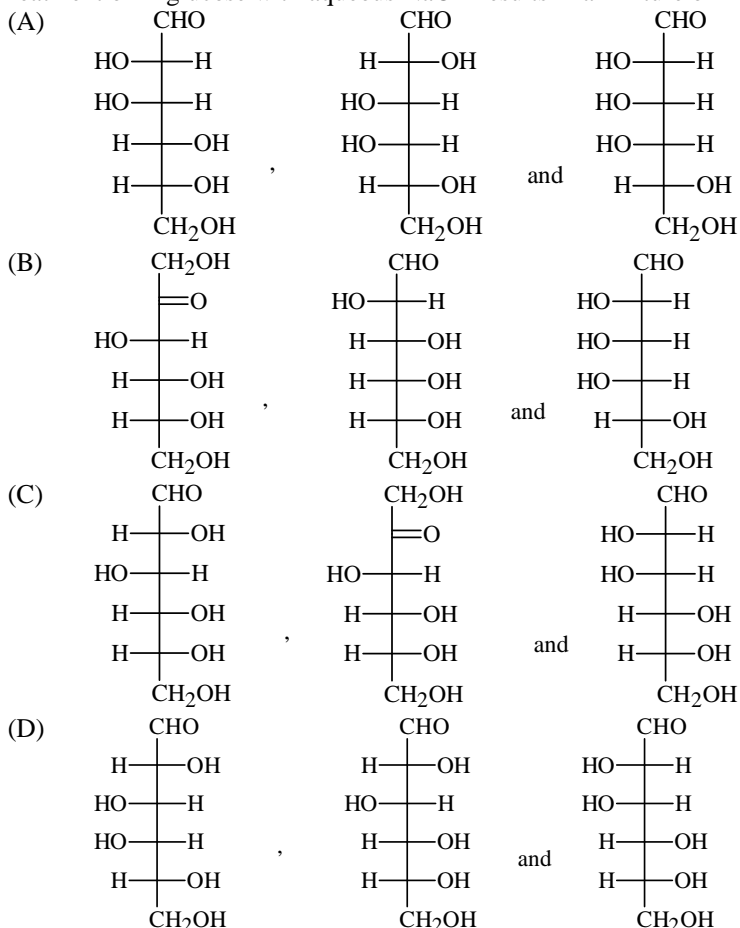
Q. 14 Among the following, the correct statement(s) about polymers is(are)

- (A) The polymerization of chloroprene gives natural rubber.
(B) Teflon is prepared from tetrafluoroethene by heating it with persulphate catalyst at high pressures.
(C) PVC are thermoplastic polymers.
(D) Ethene at 350 – 570 K temperature and 1000-2000 atm pressure in the presence of a peroxide initiator yields high density polythene.

Section 3 (Maximum Marks: 12)

- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme:
 Full Marks : +3 If **ONLY** the correct option is chosen;
 Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);
 Negative Marks : -1 In all other cases.

- Q. 15 Atom X occupies the fcc lattice sites as well as alternate tetrahedral voids of the same lattice. The packing efficiency (in %) of the resultant solid is closed to
 (A) 25 (B) 35
 (C) 55 (D) 75
- Q. 16 The reaction of HClO_3 with HCl gives a paramagnetic gas, which upon reaction with O_3 produces
 (A) Cl_2O (B) ClO_2
 (C) Cl_2O_6 (D) Cl_2O_7
- Q. 17 The reaction of $\text{Pb}(\text{NO}_3)_2$ and NaCl in water produces a precipitate that dissolves upon the addition of HCl of appropriate concentration. The dissolution of the precipitate is due to the formation of
 (A) PbCl_2 (B) PbCl_4
 (C) $[\text{PbCl}_4]^{2-}$ (D) $[\text{PbCl}_6]^{2-}$
- Q. 18 Treatment of D-glucose with aqueous NaOH results in a mixture of monosaccharides, which are



FIITJEE JEE (Advanced Paper)-2022 (PAPER-2)

ANSWER KEY

MATHEMATICS

1.	1	2.	8	3.	5	4.	1
5.	5	6.	3	7.	7	8.	6
9.	A, B	10.	A, B, C	11.	A	12.	C, D
13.	B, C, D	14.	C	15.	A	16.	A
17.	C	18.	B				

PHYSICS

1.	3	2.	2	3.	5	4.	4
5.	4	6.	3	7.	6	8.	3
9.	B	10.	A, B, C	11.	C, D	12.	A, C, D
13.	A, B	14.	B, C, D	15.	B	16.	A
17.	NONE	18.	C				

CHEMISTRY

1.	6	2.	5	3.	7	4.	2
5.	6	6.	2	7.	0	8.	2
9.	B, C	10.	B, C, D	11.	B, C	12.	A, B, C
13.	A, C	14.	B, C	15.	B	16.	C
17.	C	18.	C				

HINTS AND SOLUTIONS

MATHEMATICS

$$\begin{aligned}
 1. \quad & \frac{\sin \alpha}{\cos \beta} + \frac{\cos \alpha}{\sin \beta} + \frac{\cos \beta}{\sin \alpha} + \frac{\sin \beta}{\cos \alpha} \Rightarrow \frac{\cos(\alpha-\beta)}{\sin \beta \cos \beta} + \frac{\cos(\alpha-\beta)}{\sin \alpha \cos \alpha} \\
 & = 2 \cos(\alpha-\beta) \left[\frac{1}{\sin((\alpha+\beta)-(\alpha-\beta))} + \frac{1}{\sin((\alpha+\beta)+(\alpha-\beta))} \right] \\
 & \left[\frac{2 \times \frac{2}{3}}{\frac{1}{3} \times \frac{2}{3} - \frac{2\sqrt{2}}{3} \cdot \frac{\sqrt{5}}{3}} + \frac{2 \times \frac{2}{3}}{\frac{1}{3} \times \frac{2}{3} + \frac{2\sqrt{2}}{3} \cdot \frac{\sqrt{5}}{3}} \right] = \frac{2 \times \frac{2}{3} \times \frac{4}{9}}{\frac{4-40}{81}} \\
 & = \frac{48}{-36} = -\frac{4}{3} \Rightarrow \text{Required answer is } 1
 \end{aligned}$$

$$2. \quad y = \frac{4}{1+x^4} \Rightarrow 10y(\sqrt{2}) = 8$$

$$\begin{aligned}
 3. \quad & \int_1^2 \log_2(x^3+1) dx + \int_1^{\log_2 9} (2^x-1)^{\frac{1}{3}} dx = 2 \log_2 9 - 1 = \log_2 \left(\frac{81}{2} \right) \\
 & \text{GIF of } \log_2 \left(\frac{81}{2} \right) = 5
 \end{aligned}$$

$$\begin{aligned}
 4. \quad & (16(\log_5 x)^3 - 68 \log_5 x)(\log_5 x) = -16 \\
 & \log_5 x = t \Rightarrow 4t^4 - 17t^2 + 4 = 0 \\
 & t^2 = \frac{17 \pm \sqrt{17^2 - 8^2}}{2 \cdot 4} = \frac{17 \pm 15}{8} = 4, \frac{1}{4} \\
 & \Rightarrow \log_5 x = \pm 2, \pm \frac{1}{2} \Rightarrow x = 25, \frac{1}{25}, \sqrt{5}, \frac{1}{\sqrt{5}} \\
 & \text{Product} = 1
 \end{aligned}$$

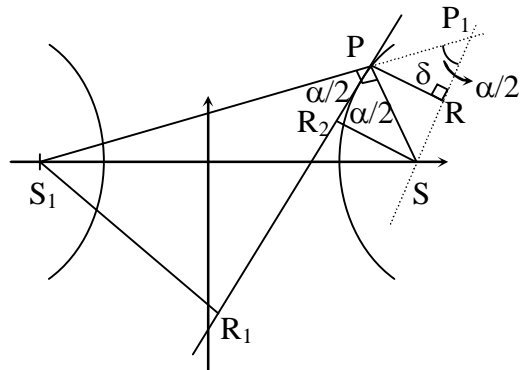
$$5. \quad \beta = \lim_{x \rightarrow 0} \frac{1+x^3 - \left(1 - \frac{x^3}{3}\right) + \left(1 - \frac{x^2}{2} - 1\right)x}{x^3} = \frac{5}{6} \Rightarrow 6\beta = 5$$

$$\begin{aligned}
 6. \quad & |A|^5 |A^2 - (\beta-1)A - \beta| = 0 \\
 & |A| \neq 0 \Rightarrow |A^2 - (\beta-1)A - \beta| = 0 \Rightarrow |A+1| |A-\beta| = 0 \\
 & |A+1| \neq 0 \Rightarrow |A-\beta| = 0 \Rightarrow \beta = \frac{1}{3} \Rightarrow 9\beta = 3
 \end{aligned}$$

7. $PR = SR_2 = \delta$

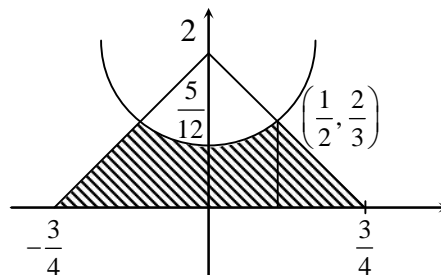
$$S_1R_1 = S_1P \sin \frac{\alpha}{2} = \beta \sin \frac{\alpha}{2}$$

$$\frac{\beta \delta}{9} \sin \left(\frac{\alpha}{2} \right) = \frac{SR_2 \cdot S_1R_1}{9} = \frac{b^2}{9} = 7$$



8.
$$9\alpha = 9 \cdot 2 \left[\int_0^{\frac{1}{2}} \left(x^2 + \frac{5}{12} \right) dx + \frac{1}{2} \cdot \frac{2}{3} \cdot \frac{1}{4} \right]$$

$$= 18 \left(\frac{1}{24} + \frac{5}{24} + \frac{2}{24} \right) = 6$$



9. In ΔPQR $\frac{\alpha}{\sin 30^\circ} = \frac{1}{\sin \theta^\circ} \Rightarrow \alpha = \frac{1}{2 \cos 10^\circ}$... (i)

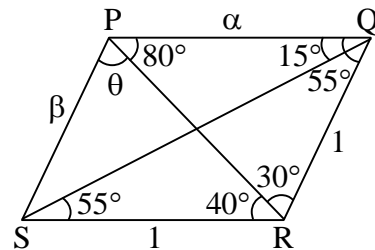
In ΔPSR $\frac{\beta}{\sin 40^\circ} = \frac{1}{\sin \theta^\circ} \Rightarrow \beta \sin \theta^\circ = \sin 40^\circ$... (ii)

From equation (i) and (ii)

$$\alpha \beta \sin \theta = \frac{\sin 40^\circ}{2 \cos 10^\circ}$$

$$4\alpha \beta \sin \theta = \frac{2 \sin 40^\circ}{\sin 80^\circ} = \frac{2 \sin 40^\circ}{2 \sin 40^\circ \cos 40^\circ} = \sec 40^\circ$$

$$\frac{2}{\sqrt{3}} < \sec 40^\circ < \sqrt{2}$$



10. So $\alpha = \sum_{k=1}^{\infty} \left(\frac{1}{2} \right)^{2k} = \frac{\frac{1}{4}}{1 - \frac{1}{4}} = \frac{1}{3}$

$$g(x) = 2^{7/3} + 2^{\frac{1-x}{3}}$$

$$\frac{2^{\frac{x}{3}} + 2^{\frac{1-x}{3}}}{2} \geq \left(2^{\frac{x}{3} + \frac{1-x}{3}} \right)^{\frac{1}{2}} \Rightarrow g(x) \geq 2^{\frac{7}{6}}$$

Also $g(x) \leq 1 + 2^{1/3}$ at $x = 0, 1$

11. Let $\omega = I_1 + iI_2 = (\bar{z})^2 + \frac{1}{z^2}$, $I_1, I_2 \in \text{Integers}$

$$\Rightarrow |\omega| = \sqrt{I_1^2 + I_2^2} = |z|^2 + \frac{1}{|z|^2}$$

$$\begin{aligned} \Rightarrow |z|^4 + \frac{1}{|z|^4} &= I_1^2 + I_2^2 - 2 \\ \Rightarrow |z|^8 - (I_1^2 + I_2^2 - 2)|z|^4 + 1 &= 0 \\ \Rightarrow |z|^4 &= \frac{(I_1^2 + I_2^2 - 2) \pm \sqrt{(I_1^2 + I_2^2 - 2)^2 - 4}}{2} \\ \Rightarrow |z| &= \left(\frac{43 \pm 3\sqrt{205}}{2} \right)^{1/4} \text{ where } I_1 = 6, I_2 = 3. \end{aligned}$$

12. $\sin\left(\frac{2\pi}{2n}\right) = \frac{r}{R+r} \Rightarrow \frac{R+r}{r} = \frac{1}{\sin\left(\frac{\pi}{n}\right)}$

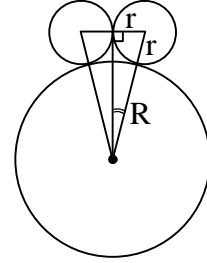
$$\frac{R}{r} + 1 = \operatorname{cosec} \frac{\pi}{n} \Rightarrow \frac{R}{r} = \left(\operatorname{cosec} \frac{\pi}{n} - 1 \right)$$

For $n = 4$, $\frac{R}{r} = (\sqrt{2} - 1) \Rightarrow R = r(\sqrt{2} - 1)$

For $n = 8$, $\frac{R}{r} > (\sqrt{2} - 1) \Rightarrow R > (\sqrt{2} - 1)r$

For $n = 5$, $\frac{R}{r} = (\operatorname{cosec} 36^\circ - 1) < 1 \Rightarrow R < r$

For $n = 12$, $\frac{R}{r} = (\operatorname{cosec} 15^\circ - 1) \Rightarrow \frac{R}{r} = (\sqrt{2}(\sqrt{3} + 1) - 1) < \sqrt{2}(\sqrt{3} + 1) \Rightarrow R < \sqrt{2}(\sqrt{3} + 1)r$



13. $\vec{a} \cdot \vec{b} = 0$

$$\Rightarrow 3 + b_2 - b_3 = 0$$

$$\Rightarrow |\vec{b}| = \sqrt{1 + b_2^2 + b_3^2}$$

$$\Rightarrow |\vec{b}| = \sqrt{2b_2^2 + 6b_2 + 10} = \sqrt{2(b_2)(b_2 + 3) + 10}$$

$$\Rightarrow |\vec{b}| = \sqrt{2b_2b_3 + 10}$$

$$\Rightarrow |\vec{b}| > 10 \quad (\because b_2b_3 > 0)$$

Also, $\vec{c} \times \vec{b} = \vec{a} - \vec{c}$

$$\Rightarrow \vec{a} \cdot \vec{b} = \vec{b} \cdot \vec{c} = 0$$

Also, $\vec{a} \cdot \vec{c} = |\vec{c}|^2 \leq |\vec{a}||\vec{c}|$

$$\Rightarrow |\vec{c}| \leq |\vec{a}| \Rightarrow |\vec{c}| \leq \sqrt{11}$$

If $\vec{a} \cdot \vec{c} = 0 \Rightarrow |\vec{c}| = 0 \Rightarrow \vec{c} = 0 \Rightarrow \vec{a} = 0$ (which is not possible)

14. $\frac{dy}{dx} + 12y = \cos\left(\frac{\pi x}{12}\right), y(0) = 0$

$$ye^{12x} = \int \cos\left(\frac{\pi x}{12}\right) e^{12x} dx$$

$$ye^{12x} = \frac{e^{12x}}{12^2 + \frac{\pi^2}{12^2}} \left[12 \cos\left(\frac{\pi x}{12}\right) + \frac{\pi}{12} \sin\left(\frac{\pi x}{12}\right) \right] + c$$

$$\Rightarrow y = \frac{1}{12^2 + \frac{\pi^2}{12^2}} \left[12 \cos\left(\frac{\pi x}{12}\right) + \frac{\pi}{12} \sin\left(\frac{\pi x}{12}\right) - 12e^{-12x} \right]$$

15. Required number of ways
 = coefficient of x^2 + coefficient of xy + coefficient of y^2 in $(3x + 3x^2 + x^3)^4 (2y + y^2)^4$
 \Rightarrow Required number of ways = $(6 \cdot 3^4) + 4 \cdot 3^3 \times 2^4 + 3^4 \times 6 \times 4 + 3^4 \times 4 \times 8 \times 4$
 = 21816

16. $M = \begin{bmatrix} \frac{5}{2} & \frac{3}{2} \\ -\frac{3}{2} & -\frac{1}{2} \end{bmatrix} = I + \frac{3}{2} \begin{bmatrix} 1 & 1 \\ -1 & -1 \end{bmatrix}$
 $A^2 = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$, where $A = \begin{bmatrix} 1 & 1 \\ -1 & -1 \end{bmatrix}$
 $\Rightarrow M^{2022} = \left(I + \frac{3}{2} A \right)^{2022} = I + \frac{3}{2} \times 2022A$
 $= \begin{bmatrix} 3034 & 3033 \\ -3033 & -3032 \end{bmatrix}$

17. $P\left(\frac{W_1}{G_{12}}\right) = \frac{P\left(\frac{W}{G}\right)}{P(G)}$
 $= \frac{\frac{5}{16} \cdot \frac{6}{32}}{\frac{5}{16} \cdot 1 + \frac{8}{16} \cdot \frac{15}{48} + \frac{3}{16} \cdot \frac{12}{16}} = \frac{15}{80 + 40 + 36} = \frac{5}{52}$

18. $f(n) = n + \sum_{r=1}^n \frac{16r + 9n - 4nr - 3n^2}{4nr + 3n^2}$
 $= \sum_{r=1}^n \frac{16r + 9n}{4nr + 3n^2}$
 $\lim_{n \rightarrow \infty} f(x) = \int_0^1 \frac{16x + 9}{4x + 3} dx$
 $= \int_0^1 4 - \frac{3}{4x + 3} dx$
 $= 4 - \frac{3}{4} \ln\left(\frac{7}{3}\right)$

PHYSICS

1.

3

\vec{F} is passing through origin, so torque of \vec{F} is zero.

So \vec{L} of the particle about O is conserved.

$$\text{So } \vec{L}_O = \left(\frac{1}{\sqrt{2}} \hat{i} + \sqrt{2} \hat{j} \right) \times (1) \left(-\sqrt{2} \hat{i} + \sqrt{2} \hat{j} + \frac{2}{\pi} \hat{k} \right)$$

$$= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{1}{\sqrt{2}} & \sqrt{2} & 0 \\ -\sqrt{2} & \sqrt{2} & \frac{2}{\pi} \end{vmatrix}$$

$$= \hat{i} \left(\frac{2\sqrt{2}}{\pi} \right) - \hat{j} \left(\frac{2}{\pi\sqrt{2}} \right) + \hat{k} (1+2) \text{ kg m}^2 \text{ s}^{-1}$$

\vec{L} at any $\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$ having velocity $\vec{v} = v_x\hat{i} + v_y\hat{j} + v_z\hat{k}$

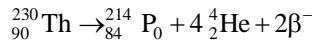
$$\vec{L} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ x & y & z \\ v_x & v_y & v_z \end{vmatrix}$$

$$= \hat{i}(yv_z - zv_y) - \hat{j}(xv_z - zv_x) + \hat{k}(xv_y - yv_x)$$

so $xy_y - yv_x = 3$

2.

2



(from convs. Of mass no and charge)

$$\text{So } \frac{n_\alpha}{n_\beta} = \frac{4}{2} = 2.$$

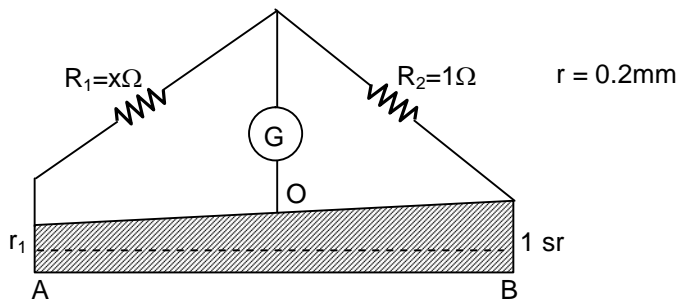
3.

5

$$R_{AO} = \int_0^{1/2} \frac{\rho}{\pi (r + 4rx)^2} dx = \frac{2\rho}{3\pi r^2}$$

$$R_{OB} = \int_{1/2}^1 \frac{\rho}{\pi (r + 4r\pi)^2} dx = \frac{2\rho}{15\pi r^2}$$

$$(x) \frac{2\rho}{15\pi r^2} = (1) \frac{2\rho}{3\pi r^2} \Rightarrow x = 5$$



4.

4

$$[B] = [e]^\alpha [M_e]^\beta [h]^\gamma [K]^\delta$$

$$[B] = M T^{-2} I^{-1}$$

$$[e] = I^T$$

$$[h] = M L^2 T^{-1}$$

$$[K] = M L^3 T^{-4} I^{-2}$$

$$MT^{-2}I^{-1} = [IT]^\alpha [M]^\beta [ML^2T^{-1}]^\gamma [ML^3T^{-4}I^{-2}]^\delta$$

$$1 = \beta + \gamma + \delta \quad (1)$$

$$-2 = \alpha - \gamma - 4\delta \quad (2)$$

$$-1 = \alpha - 2\delta \quad (3)$$

$$0 = 2\gamma + 3\delta \quad (4)$$

On solving equation (1), (2), (3) and (4), we get

$$\alpha = 3$$

$$\gamma = -3$$

$$\delta = 2$$

$$\beta = 2$$

$$\alpha + \beta + \gamma + \delta = 4$$

5. **4**

$$1 \sin 60^\circ = \frac{\sqrt{3}}{2} r$$

$$r = 45^\circ$$

$$\frac{\sqrt{3}}{2} \sin 45^\circ = \sqrt{3} \sin r_2$$

$$r_2 = 30^\circ$$

$$\left(\frac{1}{\sqrt{3}} + \frac{(\sqrt{3}-1)}{2} + \frac{(\sqrt{3}-1)}{2\sqrt{3}} \right) \times n = \frac{8}{\sqrt{3}}$$

$$n = 4.$$

6. **3**

$$\text{Flux through cone} = \frac{q}{2\epsilon_0} = \frac{nq}{6\epsilon_0}$$

$$n = 3$$

7. **6**

For $l > l_0$, it oscillates with frequency $\frac{1}{2\pi} \sqrt{\frac{k_1}{m}}$

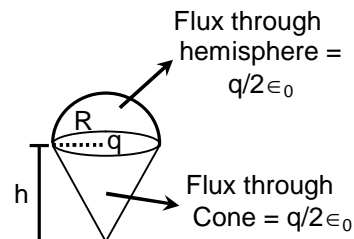
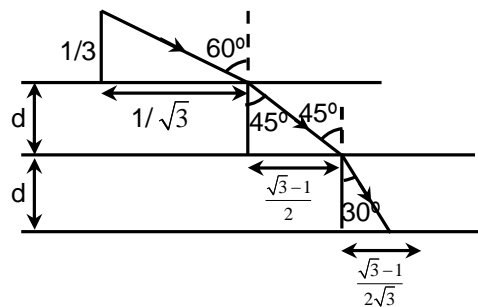
And for $l < l_0$, it oscillates with frequency $\frac{1}{2\pi} \sqrt{\frac{k_2}{m}}$

$$\text{Therefore } T = \pi \sqrt{\frac{m}{k_1}} + \pi \sqrt{\frac{m}{k_2}}$$

$$= \pi \left[\sqrt{\frac{0.1}{0.009}} + \sqrt{\frac{0.1}{0.016}} \right] = \frac{70}{12} \pi \approx 6\pi$$

$$6\pi = n\pi$$

$$n = 6$$



8. $\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$

$$\frac{1}{-x} + \frac{1}{-30} = \frac{1}{-10}$$

$$x = 15 \text{ cm}$$

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{-x} + \frac{1}{(-u)} = \frac{1}{f}$$

$$\frac{1}{x^2} \frac{dx}{dt} + \frac{1}{u^2} \frac{du}{dt} = 0$$

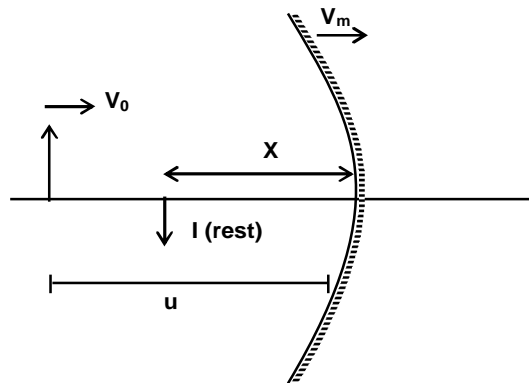
$$\frac{dx}{dt} = -\left(\frac{x}{u}\right)^2 \frac{du}{dt}$$

$$(v_m - 0) = -\left(\frac{15}{30}\right)^2 [v_m - v_0]$$

$$v_m = -\frac{1}{4}[v_m - 15]$$

$$4v_m + v_m = 15$$

$$v_m = 3 \text{ cm/s.}$$



9. for $r \in [0, 1]$; $\rho = kr$

for $r \in [1, r_B]$; $\rho = \frac{2k}{r}$

total charge of the configuration is q

$$q = \int_0^1 (kr) 4\pi r^2 dr + \int_1^{r_B} \frac{2k}{r} 4\pi r^2 dr$$

$$q = k\pi + 4k\pi(r_B^2 - 1)$$

For $r_B = \sqrt{\frac{3}{2}}$; $q = k\pi + 2k\pi = 3k\pi$

Electric field just outside B is $E = \frac{1}{4\pi\epsilon_0} \frac{(3\pi k)}{r_B^2} = \frac{k}{2\epsilon_0}$

For $r_B = \frac{3}{2}$; $q = k\pi + 5\pi k = 6k\pi$

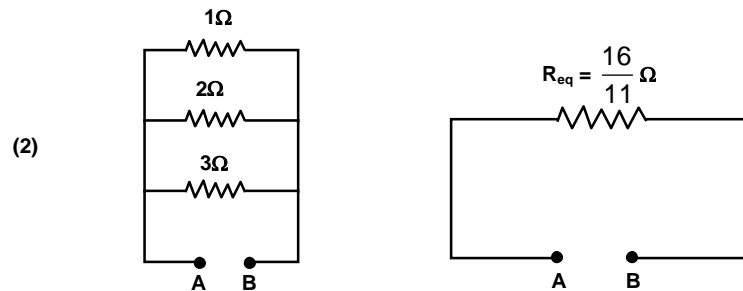
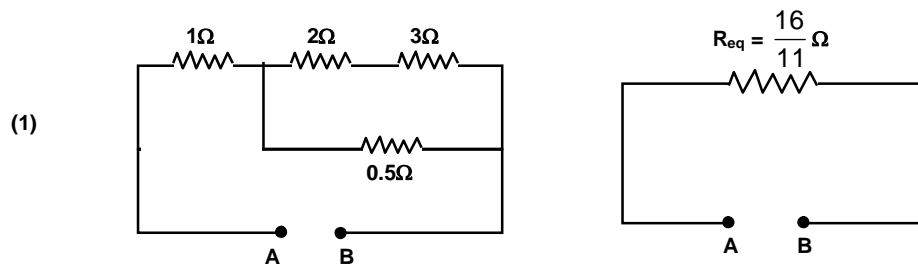
Potential just outside B is $v = \frac{(6\pi k)}{4\pi\epsilon_0 \left(\frac{3}{2}\right)} = \frac{k}{\epsilon_0}$

For $r_B = 2$; $q = k\pi + 12k\pi = 13k\pi$

For $r_B = \frac{5}{2}$; $q = k\pi + 21k\pi = 22\pi k$

Mag. of E just outside B is $\frac{1}{4\pi\epsilon_0} \frac{(22\pi k)}{\left(\frac{25}{4}\right)} = \frac{22}{25} \frac{k}{\epsilon_0}$.

10. A, B, C



If $6V$ voltage source connected to both circuit

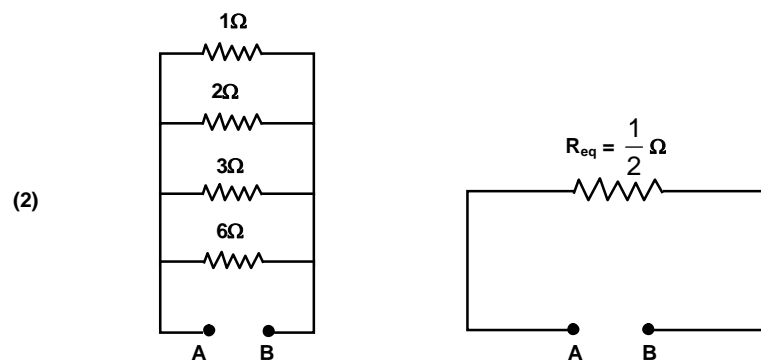
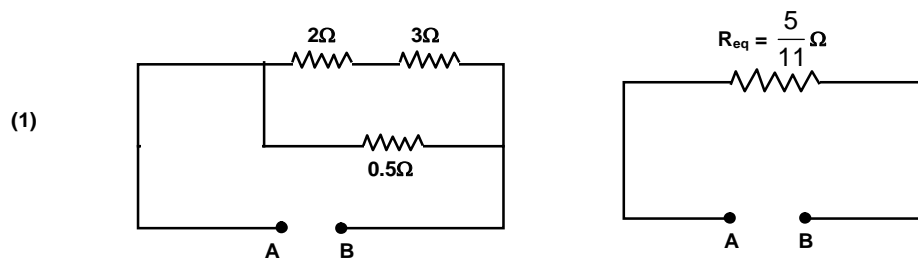
$$P \propto \frac{1}{R} \text{ voltage constant}$$

$$R_1 > R_2 \quad P_1 < P_2$$

If 2 Amp current source connected

$$P \propto R$$

$$P_1 > P_2$$



$$P_1 = \frac{6^2}{\left(\frac{16}{11}\right)} \quad Q_1 = \frac{6^2}{\left(\frac{5}{11}\right)}$$

$$Q_1 > P_1$$

$$P = i^2 R \quad R_2 > R_1 \quad \therefore Q_2 > Q_1$$

11. **C, D**

(Conducting)

Isothermal process $T = \text{constant}$

$PV = \text{constant}$

$$P_1 V_1 = P_2 V_2$$

$$\left(P_1 + \frac{4T}{R_1}\right) \frac{4}{3} \pi R_1^3 = \left(P_2 + \frac{4T}{R_2}\right) \frac{4}{3} \pi R_2^3$$

$$\left(\frac{R_1}{R_2}\right)^3 = \frac{P_2 + \frac{4T}{R_2}}{P_1 + \frac{4T}{R_1}}$$

adiabatic process $PV^\gamma = \text{constant}$ $PT^{-5/2} = \text{const.}$

(Insulating)

$$\frac{P_1^1}{P_2^1} = \left(\frac{T_2}{T_1}\right)^{5/2}$$

$$\left(\frac{T_2}{T_1}\right)^{5/2} = \frac{\left(P_1 + \frac{4T}{R_1}\right)}{\left(P_2 + \frac{4T}{R_2}\right)}$$

12. **A, C, D**

$$\vec{F}_1 = \frac{q\sigma}{2\epsilon_0} \left(1 - \frac{Z}{\sqrt{R^2 + Z^2}}\right) \hat{k}$$

$$\vec{F}_2 = -c\hat{k}$$

$$\beta = \frac{1}{4} \quad \therefore \frac{1}{4} = \frac{2c\epsilon_0}{q\sigma} \quad (\text{Given})$$

$$\frac{q\sigma}{2\epsilon_0} = 4c \quad \dots (1)$$

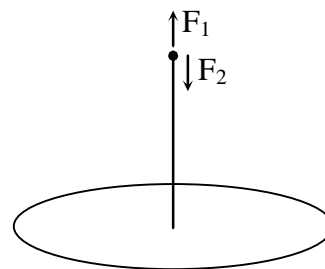
For equilibrium at $z = Z_0$

$$F_1 = F_2 \Rightarrow \frac{q\sigma}{2\epsilon_0} \left(1 - \frac{Z}{\sqrt{R^2 + Z^2}}\right) = c \text{ from equation (1)}$$

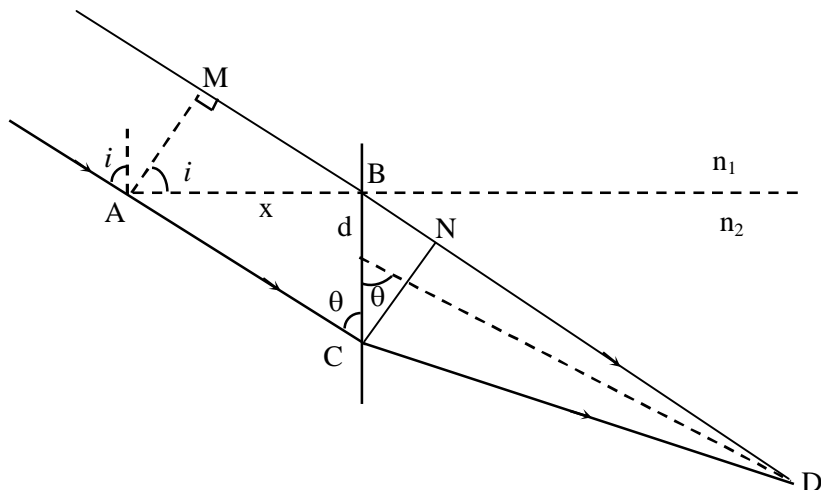
$$\Rightarrow \left(1 - \frac{Z}{\sqrt{R^2 + Z^2}}\right) = \frac{1}{4} \Rightarrow \frac{Z}{\sqrt{R^2 + Z^2}} = \frac{3}{4} \Rightarrow Z = \sqrt{\frac{9}{7}} R \approx 1.13R$$

$Z > 1.13R$; $F_2 > F_1$ Particle reaches origin

$Z < 1.13R$; $F_1 > F_2$ Particle reaches back to $z = Z_0$



13. A, B



Path difference

$$\Delta r = (MB + BN) - AC$$

$$\Delta r = (n_1 x \sin i + n_2 d \cos \theta) - \frac{n_2 d}{\cos \theta}$$

$$\Delta r = n_1 (d \tan \theta) \frac{n_2}{n_1} \sin \theta + n_2 d \cos \theta - \frac{n_2 d}{\cos \theta} \quad (\because x = d \tan \theta ; n_1 \sin i = n_2 \sin \theta)$$

$$\Delta r = \frac{n_2 d \sin^2 \theta}{\cos \theta} + n_2 d \cos \theta - \frac{n_2 d}{\cos \theta}$$

$$\Delta r = \frac{n_2 d [\sin^2 \theta + \cos^2 \theta - 1]}{\cos \theta} = 0$$

14. B, C, D

Volume of gas at B is

$$V_B = \left(\frac{100}{300} \right)^{3/5} (0.8) = 0.4 \text{ m}^3$$

$$W_{AB} = \frac{P_A V_A - P_B V_B}{\gamma - 1} = -60 \text{ kJ}$$

$$W_{BC} = P_B V_B \ln 2 = 84 \text{ kJ}$$

$$W_{CA} = 0$$

15.

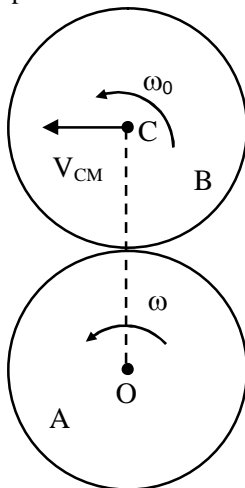
B

$$V_{CM} = 2R\omega$$

At point of contact

$$V_{CM} = \omega_0 R \Rightarrow \omega_0 = 2\omega$$

Angular momentum of disk B with respect to centre of A is



$$L = \left(\frac{MR^2}{2} \right) (\omega_0) + M(2R\omega)(2R)$$

$$= \left(\frac{MR^2}{2} \right) (2\omega) + 4MR^2\omega$$

$$L = 5MR^2\omega \therefore n = 5.$$

16.

A

$$6e = \frac{hc}{\lambda} - \phi_0$$

$$0.6e = \frac{hc}{4\lambda} - \phi_0$$

Solving the above 2 equations, we get (A)

17.

None

$$L.C. = \frac{0.5}{100} = .005 \text{ mm}$$

$$\text{I } 4 \times 0.25 + (20 - 4) \times .005 \rightarrow 1.08 \text{ mm}$$

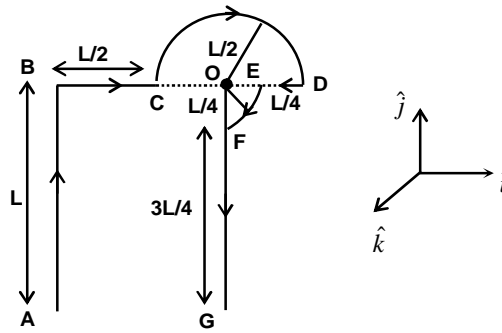
$$\text{II } 4 \times 0.25 + (16 - 4) \times .005 \rightarrow 1.06 \text{ mm}$$

$$d_m = \frac{1.06 + 1.08}{2} = 1.07$$

$$\Delta d_m = \frac{.01 + .01}{2} = .01$$

$$d = (1.07 \pm .01) \text{ mm.}$$

18. C



$$\vec{B}_{\text{Net}} = \vec{B}_{AB} + \vec{B}_{BC} + \vec{B}_{CD} + \vec{B}_{DE} + \vec{B}_{EF} + \vec{B}_{FG}$$

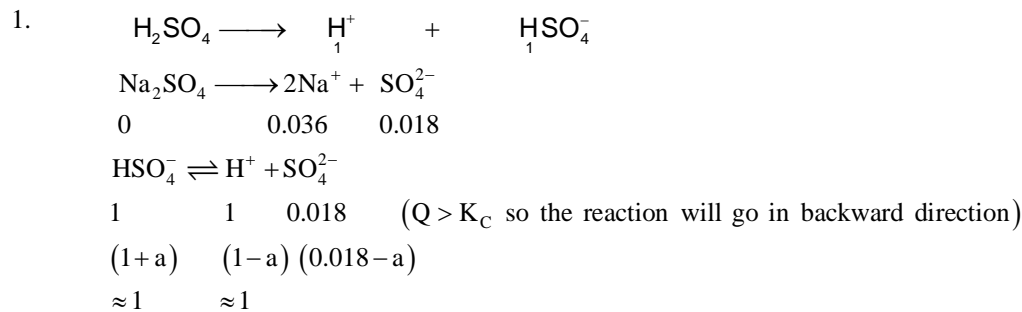
$$\vec{B}_{AB} = \vec{B}_{DE} = \vec{B}_{FG} = 0$$

$$\vec{B}_{AB} = \frac{\mu_0 I}{4\pi L} \sin 45^\circ [-\hat{k}]$$

$$\vec{B}_{CD} = \frac{\mu_0 I}{4\left(\frac{L}{2}\right)} [-\hat{k}]$$

$$\vec{B}_{EF} = \frac{\mu_0 I}{8\left(\frac{L}{4}\right)} [-\hat{k}] \Rightarrow \text{(C)}$$

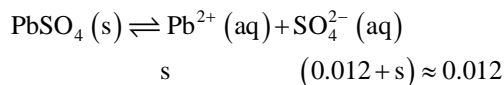
CHEMISTRY



$$\text{Now, } 0.012 = \frac{1 \times (0.018 - a)}{1}$$

$$a = 0.006$$

$$[\text{SO}_4^{2-}] = 0.018 - 0.006 = 1.2 \times 10^{-2} \text{ M}$$



$$s = \frac{1.6 \times 10^{-8}}{0.012} = 1.33 \times 10^{-6}$$

$$\therefore y = 6$$

2.
$$\frac{P^\circ - P_s}{P^\circ} = iX_B$$

$$\frac{60 - 59.724}{60} = i \times \frac{0.1}{0.1 + 100}$$

$$\frac{0.276}{60} = i \times \frac{0.1}{100.1} = i \times \frac{1}{1000}$$

$$i = \frac{276}{60} = 4.6$$

$$i = 1 + (n-1)\alpha$$

$$4.6 = 1 + (n-1)0.9$$

$$n = 5$$

3. Let λ_m^0 the molar conductance by $Z_m X_n$

From the graph

$$339 = \lambda_m^0 - b\sqrt{c}$$

$$339 = \lambda_m^0 - b \times 0.01 \quad \dots(1)$$

$$336 = \lambda_m^0 - b \times 0.04 \quad \dots(2)$$

On solving, we get, $\lambda_m^0 = 340$

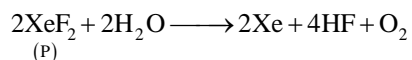
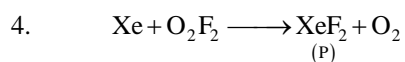
$$\text{Now, } 25m + 100p = 250 \quad \dots(3)$$

$$100m + 80n = 440 \quad \dots(4)$$

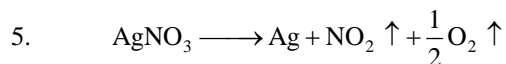
$$50m + 80n = 340 \quad \dots(5)$$

On solving (3), (4) and (5)

We get, $m = 2, n = 3, p = 2$



Per mol of P, 2 moles of HF will be formed.



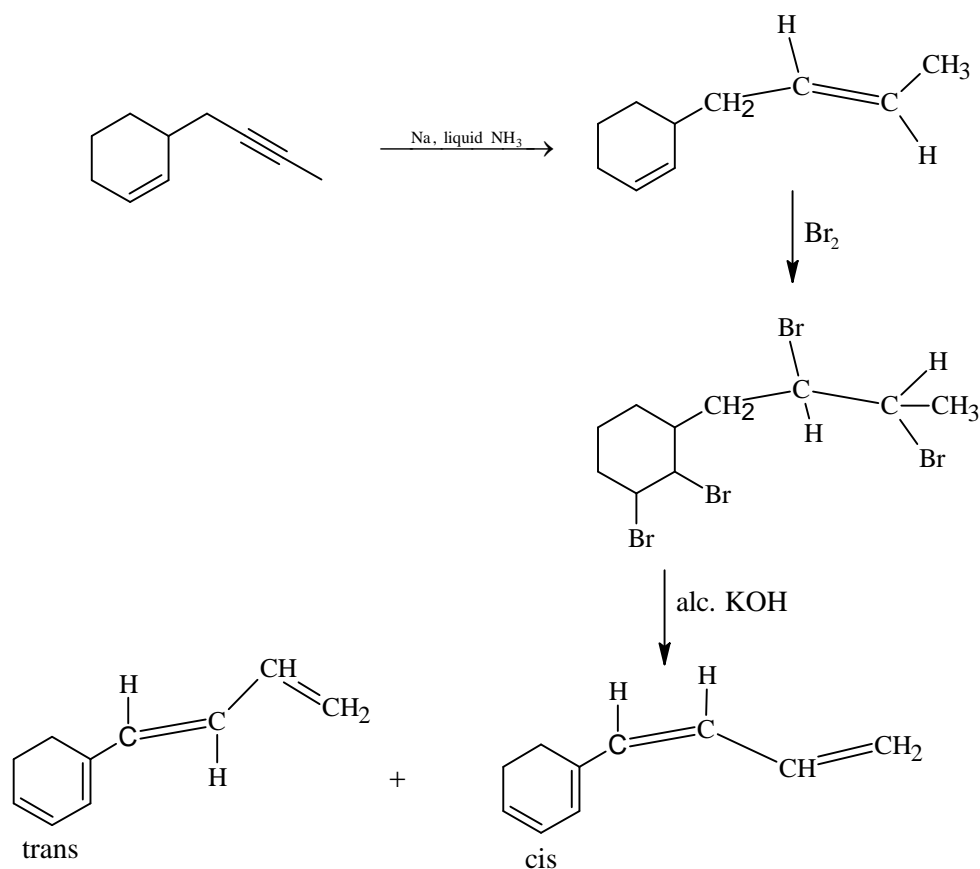
$\text{NO}_2 \longrightarrow$ One unpaired electron

$\text{O}_2 \longrightarrow$ Two unpaired electrons

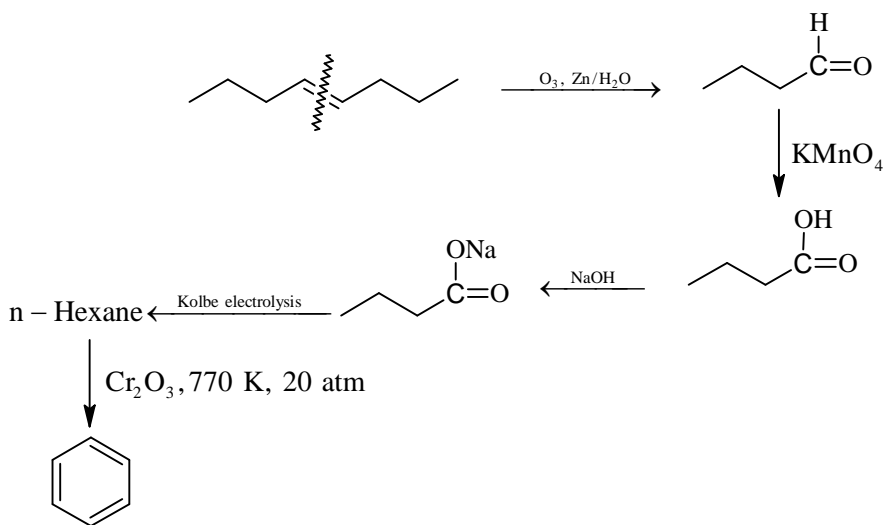
$$\sigma 1s^2 < \sigma 1s^{*2} < \sigma 2s^2 < \sigma 2s^{*2} < \sigma 2p_z^2 < \pi 2p_x^2 = \pi 2p_y^2 < \pi 2p_x^{*1} = \pi 2p_y^{*1}$$

Number of antibonding electron in $\text{O}_2 = 6$.

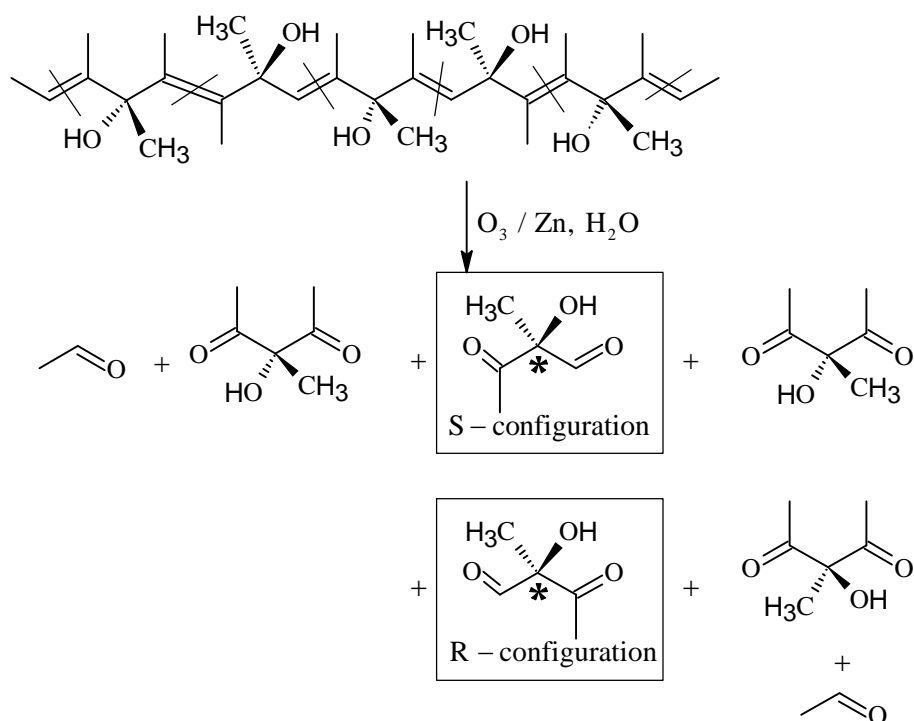
6.



7.



8.



- Only 2-chiral molecules are formed.
9. As per the law of multiple proportion, if P and Q form two or more compounds, then the ratio of the masses of one of the element (P) that combines with fix mass of Q bear a simple whole number ratio.
- Now

Compound	% of P	% of Q
1	50	50
2	44.4	55.6
3	40	60

OR

Compound	% of P	% of Q
1	50	50
2	40	50
3	33.33	50

(A) Given that formula of compound 3 is P_3Q_4 and that of compound 2 is P_3Q_5
Then compound 3 $\Rightarrow P_{15/4} Q_5$

Compound 2 $\Rightarrow P_3 Q_5$

So, ratio of masses of P in 3 and 2 which combines with fixed mass of

$$Q = \frac{15}{4} : 3 = \frac{5}{4}$$

But from table 2, ratio of masses of P in 3 and 2 = $\frac{33.33}{40} = \frac{5}{6}$

Since two ratio are not same, so option (A) is incorrect.

(B) Empirical formula of compound

P	$\frac{40}{20} = 2$	$\frac{3}{2}$
Q	$\frac{60}{45} = \frac{4}{3}$	1

So, empirical formula of compound 3 is P_3Q_2

(C) Compound 2 $\Rightarrow PQ$ or P_4Q_4

Compound 3 $\Rightarrow P_5Q_4$

So, ratio of masses of P in 2 and 3 which combines with fix mass of Q is = 4 : 5 which resembles table 2.

(D) Empirical form of compound should be PQ_2 and not P_2Q

10. (A) $\Delta S = nF \left(\frac{\partial E_{\text{cell}}}{\partial T} \right)$
 $= nF \times \frac{R}{F} = nR = 2R (\because n = 2)$

Incorrect statement.

(B) E_{cell} for the given cell is +ve.

$\therefore \Delta G = -ve$

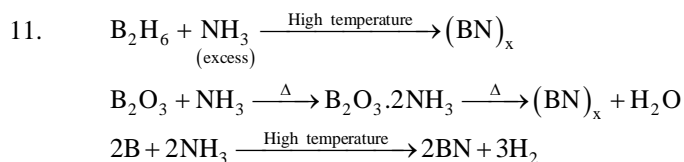
Since, $\Delta S = nF \left(\frac{\partial E_{\text{cell}}}{\partial T} \right)$

$\therefore \Delta S = +ve$

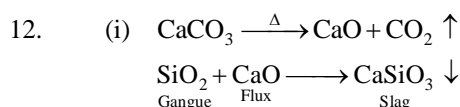
Correct statement.

(C) Correct statement because racemisation involves formation of a racemic mixture.

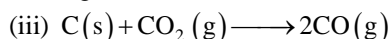
(D) Correct statement because number of particles are increasing.



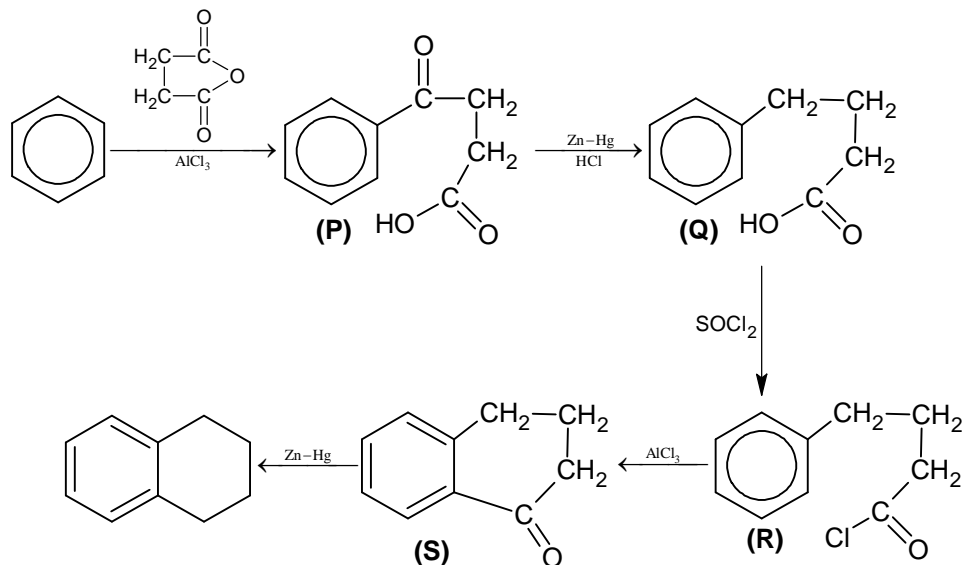
Since, Boron is not a compound, so option (A) is not correct.



(ii) Pig iron contains 4% of carbon.



13.



14. (i) Polymerization of chloroprene gives synthetic rubber.
 (ii) PVC is thermoplastic polymer.
 (iii) Ethene at 350 – 570 K temperature and 1000 – 2000 atm pressure in presence of peroxide initor yields low density polythene.

15.
$$X = 8 \times \frac{1}{8} + 6 \times \frac{1}{2} + \frac{1}{2} \times 8$$

$$= 1 + 3 + 4 = 8$$

$$2r = \frac{\sqrt{3}}{4} a;$$

$$r = \frac{\sqrt{3}}{8} a$$

$$\text{Packing fraction} = \frac{\text{number of atoms} \times \text{volume of one atom}}{\text{volume of unit cell}} \times 100\%$$

$$= \frac{8 \times \frac{4}{3} \times 3.14 \times \left(\frac{\sqrt{3}}{8} a\right)^3}{a^3} \times 100\%$$

$$= 35\%$$

16. $\text{ClO}_3^- + \text{Cl}^- \longrightarrow \text{ClO}_2$
 $2\text{ClO}_2 + 2\text{O}_3 \longrightarrow \text{Cl}_2\text{O}_6 + 2\text{O}_2$
17. $\text{Pb}(\text{NO}_3)_2 + 2\text{NaCl} \longrightarrow \text{PbCl}_2 \downarrow$
 $\text{PbCl}_2 + 2\text{HCl} \longrightarrow [\text{PbCl}_4]^{-2}$

18. [Lobry-de-Bruyn-Van Ekenstein rearrangement]

