Note: For the benefit of the students, specially the aspiring ones, the question of JEE(advanced), 2017 are also given in this booklet. Keeping the interest of students studying in class XI, the questions based on topics from class XI have been marked with '*', which can be attempted as a test. For this test the time allocated in Physics, Chemistry & Mathematics are 22 minutes, 21 minutes and 25 minutes respectively.



PAPER-2

P2-17-6-1

Time : 3 Hours

Maximum Marks : 183

CODE

COVER PAGE IS AS PER THE ACTUAL PAPER

READ THE INSTRUCTIONS CAREFULLY

GENERAL

- 1. This sealed booklet is your Question Paper. Do not break the seal till you are told to do so.
- 2. The paper CODE is printed on the right hand top corner of this sheet and the right hand top corner of the back cover of this booklet.
- 3. Use the Optical Response Sheet (ORS) provided separately for answering the questions.
- 4. The paper CODE is printed on the left part as well as the right part of the ORS. Ensure that both these codes are identical and same as that on the question paper booklet. If not, contact the invigilator for change of ORS.
- 5. Blank spaces are provided within this booklet for rough work.
- 6. Write your name, roll number and sign in the space provided on the back cover of this booklet.
- 7. After breaking the seal of the booklet at **2:00 pm**, verify that the booklet contains **36** pages and that all the **54** questions along with the options are legible. If not, contact the invigilator for replacement of the booklet.
- 8. You are allowed to take away the Question Paper at the end of the examination.

OPTICAL RESPONSE SHEET

- 9. The ORS (top sheet) will be provided with an attached Candidate's Sheet (bottom sheet). The Candidate's Sheet is a carbonless copy of the ORS.
- 10. Darken the appropriate bubbles on the ORS by applying sufficient pressure. This will leave an impression at the corresponding place on the Candidate's Sheet.
- 11. The ORS will be collected by the invigilator at the end of the examination.
- 12. You will be allowed to take away the Candidate's Sheet at the end of the examination.
- 13. Do not tamper with or mutilate the ORS. Do not use the ORS for rough work.
- 14. Write your name, roll number and code of the examination center, and sign with pen is the space provided for this purpose on the ORS. **Do not write any of these details anywhere else** on the ORS. Darken the appropriate bubble under each digit of your roll number.

DARKENING THE BUBBLES ON THE ORS

- 15. Use a **BLACK BALL POINT PEN** to darken the bubbles on the ORS.
- 16. Darken the bubble **COMPLETELY**.
- 17. The correct way of darkening a bubble is as:
- 18. The ORS is machine-gradable. Ensure that the bubbles are darkened in the correct way.
- 19. Darken the bubbles **ONLY IF** you are sure of the answer. There is **NO WAY** to erase or "un-darken" a darkened bubble. Please see the last page of this booklet for rest of the instruction.

PART I: PHYSICS

| | SECTION 1 (Maximum Marks: 21) | | | | |
|---|--|-------|--------|--|--|
| • | This section con- | tains | s SEVI | CN questions. | |
| • | Each question has FOUR options [A], [B], [C] and [D]. ONLY ONE of these four options is correct. | | | | |
| • | For each question, darken the bubble(s) corresponding to all the correct option(s) in the ORS. | | | | |
| • | For each question, marks will be awarded in one of the following categories: | | | | |
| | Full Marks | : | + 3 | If only the bubble(s) corresponding to the correct option is darkened. | |
| | Zero Marks | : | 0 | If none of the bubbles is darkened. | |
| | Negative Marks | : | - 1 | In all other cases. | |
| | Negative Marks | : | - 1 | In all other cases. | |

*Q.1 Consider an expanding sphere of instantaneous radius R whose total mass remains constant. The expansion is such that the instantaneous density ρ remains uniform throughout the volume. The rate of fractional change in density $\left(\frac{1}{\rho}\frac{d\rho}{dt}\right)$ is constant. The velocity v of any point on the surface of the expanding sphere is

| | · · | , | |
|-------------------|-----|---|------------------------------------|
| proportional to | | | |
| [A] R | | | [B] R ³ |
| $[C] \frac{1}{P}$ | | | [D] R ² |

Sol.

A

(

$$m = \rho \frac{4}{3} \pi R^{3}$$

$$0 = \rho \cdot 4\pi R^{2} \frac{dR}{dt} + \frac{4}{3} \pi R^{3} \frac{d\rho}{dt}$$

$$-\frac{1}{\rho} \frac{d\rho}{dt} = \frac{3}{R} \frac{dR}{dt}$$

$$-\frac{R}{3} \frac{1}{\rho} \frac{d\rho}{dt} = \frac{dR}{dt}$$

$$\frac{dR}{dt} \propto R$$

$$v \propto R$$

*Q.2 Consider regular polygons with number of sides $n = 3, 4, 5, \dots$ as shown in the figure. The center of mass of all the polygons is at height h from the ground. They roll on a horizontal surface about the leading vertex without slipping and sliding as depicted. The maximum increase in height of the locus of the center of mass for each polygon is Δ . Then Δ depends on n and h as



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Q.3 A photoelectric material having work-function ϕ_0 is illuminated with light of wavelength $\lambda \left(\lambda < \frac{hc}{\phi_0}\right)$. The

fastest photoelectron has a de Broglie wavelength λ_d . A change in wavelength of the incident light by $\Delta\lambda$ results in change $\Delta\lambda_d$ in λ_d . then the ratio $\Delta\lambda_d / \Delta\lambda$ is proportional to [A] λ_d / λ [B] λ_d^2 / λ

| - | | | | - | u |
|----|-----|-----------------------|----|-----|---------------------------|
| [C |)) | ι_d^3 / λ | [[|))) | λ_d^3 / λ^2 |

Sol.

D

$$\frac{P^{2}}{2m} = \frac{hc}{\lambda} - \phi_{0}$$
$$\frac{h^{2}}{2m \lambda_{D}^{2}} = \frac{hc}{\lambda} - \phi_{0}$$
$$- \frac{h^{2}}{m} \frac{1}{\lambda_{D}^{3}} d\lambda_{D} = \frac{hc}{\lambda^{2}} d\lambda$$
$$\frac{\Delta \lambda_{D}}{\Delta \lambda} \propto \frac{\lambda_{D}^{3}}{\lambda^{2}}.$$

Q.4 A symmetric star conducting wire loop is carrying a steady state current I as shown in figure. The distance between the diametrically opposite vertices of the star is 4a. The magnitude of the magnetic field at the center of the loop is



*Q.5 Three vectors \vec{P} , \vec{Q} and \vec{R} are shown in the figure. Let S be any point on the vector \vec{R} . The distance between the point P ad S is $b | \vec{R} |$. The general relation among vectors \vec{P} , \vec{Q} and \vec{S} is



Sol.

Α

 $\vec{S} - \vec{P} = b\vec{R}$ and $\vec{Q} - \vec{S} = (1 - b)\vec{R}$ where $\vec{R} = \vec{Q} - \vec{P}$ From these two equations $\vec{S} = (1 - b)\vec{P} + b\vec{Q}$

*Q.6 A rocket is launched normal to the surface of earth, away from the Sun, along the line joining the Sun and the Earth. The Sun is 3×10^5 times heavier than the Earth and is at a distance 2.5×10^4 times larger than the radius of the Earth. The escape velocity from Earth's gravitational field is $v_e = 11.2$ km s⁻¹. The minimum initial (v_s) required for the rocket to be able to leave the Sun-earth system is closest to (Ignore the rotation and revolution of the Earth and the presence of any other planet) [A] $v_s = 22$ km s⁻¹ [B] $v_s = 42$ km s⁻¹ [C] $v_s = 62$ km s⁻¹ [D] $v_s = 72$ km s⁻¹

Sol.

B

$$\begin{split} &\frac{1}{2}mv_{es}^2-\frac{GMm}{R}-\frac{G(3\times10^5M)\times m}{2.5\times10^4R}=0\\ &\Rightarrow \quad V_{es}=\sqrt{13} \quad v_e=40.3 \text{ km/s} \end{split}$$

Q.7 A person measures the depth of a well by measuring the time interval between dropping a stone and receiving the sound of impact with the bottom of the well. The error in his measurement of time is $\delta T = 0.01$ seconds and he measures the depth of the well to be L = 20 meters. Take the acceleration due to gravity g = 10 ms⁻² and the velocity of sound is 300 ms⁻¹. Then the fractional error in the measurement, $\delta L/L$, is closest to
[A] 0.2 %
[B] 1 %
[C] 3 %
[D] 5 %

B

$$t = \sqrt{\frac{2L}{g}} + \frac{L}{C}$$
$$\frac{dt}{dL} = \sqrt{\frac{L}{g}} \times \frac{1}{2\sqrt{L}} + \frac{1}{C}$$

$$dL = \frac{dt}{\frac{1}{\sqrt{2gL}} + \frac{1}{C}}$$
$$\Rightarrow \quad \frac{dL}{L} \times 100 = \left(\frac{dt}{\frac{1}{\sqrt{2gL}} + \frac{1}{C}}\right) \frac{1}{L} \times 100$$
$$= \frac{15}{16\%} \approx 1\%$$

SECTION 2 (Maximum Marks: 28)

- This section contains SEVEN questions.
- Each question has **FOUR** options [A], [B], [C] and [D]. **ONE OR MORE THAN ONE** of these four options is(are) correct.
- For each question, darken the bubble(s) corresponding to all the correct option(s) in the ORS.
- For each question, marks will be awarded in one of the following categories:

| Full Marks | : | + 4 | If only the bubble(s) corresponding to all the correct option(s) is(are) darkened. |
|----------------|---|-----|--|
| Partial Marks | : | + 1 | For darkening a bubble corresponding to each correct option, provided NO |
| | | | incorrect option is darkened. |
| Zero Marks | : | 0 | If none of the bubbles is darkened. |
| Negative Marks | : | - 2 | In all other cases. |

- For example, if [A], [C] and [D] are all the correct options for a question, darkening all these three will get +4 marks; darkening only [A] and [D] will get +2 marks; and darkening [A] and [B] will get -2 marks, as a wrong option is also darkened.
- Q.8 A uniform magnetic field B exists in the region between x = 0 and $x = \frac{3R}{2}$ (region 2 in the figure) pointing normally into the plane of the paper. A particle with charge +Q and momentum p directed along x-axis enters region 2 from region 1 at point P₁ (y = -R). Which of the following option(s) is/are correct?

- [A] For $B > \frac{2}{3} \frac{p}{QR}$, the particle will re-enter region 1
- [B] For $B = \frac{8}{13} \frac{p}{QR}$, the particle will enter region 3 through the point P₂ on x-axis
- [C] When the particle re-enters region 1 through the longest possible path in region 2, the magnitude of the change in its linear momentum between point P₁ and the farthest point from y-axis is $p/\sqrt{2}$
- [D] For a fixed B, particles of same charge Q and same velocity v, the distance between the point P_1 and the point of re-entry into region 1 is inversely proportional to the mass of the particle

Sol.

A, B

$$R' = \frac{p}{qB}$$

$$(R' - R)^{2} + R^{2} = R'$$

$$\Rightarrow R' = \frac{13}{8}R$$

$$R' - R$$

$$R'$$

Q.9 The instantaneous voltages at three terminals marked X, Y and Z are given by $V_x = V_0 \sin \omega t$

$$V_{y} = V_{0} \sin\left(\omega t + \frac{2\pi}{3}\right) \text{ and}$$
$$V_{z} = V_{0} \sin\left(\omega t + \frac{4\pi}{3}\right).$$

An ideal voltmeter is configured to read rms value of the potential difference between its terminals. It is connected between points X and Y and then between Y and Z. The reading(s) of the voltmeter will be

[A] $V_{XY}^{rms} = V_0 \sqrt{\frac{3}{2}}$ [B] $V_{YZ}^{rms} = V_0 \sqrt{\frac{1}{2}}$

$$[C] \quad V_{XY}^{rms} = V_0$$

Sol.

[D] independent of the choice of the two terminals

A, D

$$V_{XYO} = V_{Y2O} = V_{ZXO} = \sqrt{3}V_0$$

 $V_{XX}^{rms} = V_{YZ}^{rms} = \sqrt{\frac{3}{2}}V_0$

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 V_0

Q.10 A point charge +Q is placed just outside an imaginary hemispherical surface of radius R as shown in the figure. Which of the following statements is/are correct?



- [A] The electric flux passing through the *curved* surface of the hemisphere is $-\frac{Q}{2\varepsilon_0}\left(1-\frac{1}{\sqrt{2}}\right)$
- [B] Total flux through the curved and the flat surfaces is $\frac{Q}{Q}$
- [C] The component of the electric field normal to the flat surface is constant over the surface
- [D] The circumference of the flat surface is an equipotential

Sol. A, D

Solid angle subtended by flat surface at position of charge $-2\pi(1 - \cos \theta)$

$$= 2\pi(1 - \cos\theta)$$
$$= 2\pi(1 - \cos 45^\circ)$$
$$= 2\pi\left(1 - \frac{1}{\sqrt{2}}\right)$$

Flux entering through curved surface = flux leaving through flat surface

$$\Rightarrow \text{ Flux entering through curved surface} = -\frac{Q}{\varepsilon_0} \times \frac{1}{4\pi} \times 2\pi \left(1 - \frac{1}{\sqrt{2}}\right)$$

$$= -\frac{Q}{2\epsilon_0} \left(1 - \frac{1}{\sqrt{2}}\right)$$

Also all points of circumference are at equal distance from the charge

Q.11 Two coherent monochromatic point sources S_1 and S_2 of wavelength $\lambda = 600$ nm are placed symmetrically on either side of the centre of the circle as shown. The sources are separated by a distance d = 1.8 mm. This arrangement produces interference fringes visible as alternate bright and dark spots on the circumference of the circle. The angular separation between two consecutive bright spots is $\Delta \theta$. Which of the following options is/are correct?



- [A] A dark spot will be formed at the point P_2
- [B] At P₂ the order of the fringe will be maximum
- [C] The total number of fringes produced between P1 and P2 in the first quadrant is close to 3000
- [D] The angular separation between two consecutive bright spots decreases as we move from P_1 to P_2 along the first quadrant







Q.12 A source of constant voltage V is connected to a resistance R and two ideal inductors L_1 and L_2 through a switch S as shown. There is no mutual inductance between the two inductors. The switch S is initially open. At t = 0, the switch is closed and current begins to flow. Which of the following options is/are correct?



A, B, C Let current through R, L₁ and L₂ is i, i₁ and i₂ respectively L₁i₁ = L₂i₂ ...(i) i₁ + i₂ = i = $\frac{V}{R}$...(ii) After long time Solving, i₁ = $\frac{L_2}{L_1 + L_2} \cdot \frac{V}{R}$, i₂ = $\frac{L_1}{L_1 + L_2} \cdot \frac{V}{R}$

Sol.

*Q.13 A rigid uniform bar AB of length L is slipping from its vertical position on a frictionless floor (as shown in the figure). At some instant of time, the angle made by the bar with the vortical is θ . Which of the following statements about its motion is/are correct?



- [A] The midpoint of the bar will fall vertically downward
- [B] The trajectory of the point A is a parabola
- [C] Instantaneous torque about the point in contact with the floor is proportional to sin θ
- [D] When the bar makes an angle θ with the vertical, the displacement of its midpoint from the initial position is proportional to $(1-\cos \theta)$
- Sol. A, C, D
 - There is no horizontal force on rod during its motion
 - \Rightarrow C.M. will fall vertically downwards
 - Net torque about point B(on the ground) = mgL sin θ
 - Displacement mid point $=\frac{L}{2}-\frac{L}{2}\cos\theta$
- *Q.14 A wheel of radius R and mass M is placed at the bottom of a fixed step of height R as shown in the figure. A constant force is continuously applied on the surface of the wheel so that it just climbs the step without slipping. Consider the torque τ about an axis normal to the plane of the paper passing through the point Q. Which of the following options is/are correct?



- [A] If the force is applied at point P tangentially then τ decreases continuously as the wheel climbs
- [B] If the force is applied normal to the circumference at point X then τ is constant
- [C] If the force is applied normal to the circumference at point P then τ is zero
- [D] If the force is applied tangentially at point S then $\tau \neq 0$ but the wheel never climbs the step

Sol. A

• As the force acts as shown and considering its direction to be constant, then $\tau_{net} = F(2R \cos \theta) - mgR \cos \theta = R \cos \theta(2F-mg)$ Which definitely infers that as θ increases, τ_{net} decreases.

• As soon as force is applied as shown, it leads to frictional force between bottom point and horizontal surface, which will produce non-zero torque about point Q.





SECTION 3 (Maximum Marks : 12)

- This section contains TWO paragraphs
- Based on each table, there are **TWO** questions
- Each question has FOUR options [A], [B], [C], and [D]. ONLY ONE of these four options is correct
- For each question, darken the bubble corresponding to the correct option in the ORS
- For each question, marks will be awarded in <u>one of the following catogories</u>:

Full Marks: +3If only the bubble corresponding to the correct option is darkenedZero Marks: 0In all other cases

PARAGRAPH 1

Consider a simple RC circuit as shown in Figure 1. Process 1: In the circuit the switch S is closed at t = 0 and the capacitor is fully charged to voltage V₀ (i.e. charging continues for time T >> RC). In the process some dissipation (E_D) occurs across the resistance R. The amount of energy finally stored in the fully charged capacitor is E_C. Process 2: In a different process the voltage is first set to $\frac{V_0}{3}$ and maintained for a charging time T>> RC. Then the voltage is raised to $\frac{2V_0}{3}$ without discharging the capacitor and again maintained for time T >> RC. The process is repeated one more time by raising the voltage to V₀ and the capacitor is charged to the same final



Q.15. In Process 1, the energy stored in the capacitor E_C and heat dissipated across resistance E_D are released by: [A] $E_C = E_D$ [B] $E_C = E_D \ln 2$

[C]
$$E_{\rm C} = \frac{1}{2}E_{\rm D}$$
 [D] $E_{\rm C} = 2E_{\rm D}$

Sol.

A

$$W_{b} = CV_{0} \times V_{0}$$
$$\Delta U = \frac{1}{2}CV_{0}^{2} = E_{C}$$

Heat dissipated = $W_b - E_C$ or $E_C = E_D = \frac{1}{2}CV_0^2$

Q.16 In Process 2, total energy dissipated across the resistance E_D is:

[A]
$$E_D = \frac{1}{2}CV_0^2$$

[B] $E_D = 3\left(\frac{1}{2}CV_0^2\right)$
[C] $E_D = \frac{1}{3}\left(\frac{1}{2}CV_0^2\right)$
[D] $E_D = 3CV_0^2$

Sol.

С

If capacitor is charged from $\,V_i$ to $\,V_f$; heat dissipated is $\,H=W_{battery}-\Delta U\,$

$$= C(V_f - V_i)V_f - \left[\frac{1}{2}C(V_f^2 - V_i^2)\right]$$
$$= \frac{1}{2}C(V_f - V_i)^2$$

Total heat dissipated

$$= \frac{1}{2} C \left\{ \left(\frac{V_0}{3} - 0 \right)^2 + \left(\frac{2V_0}{3} - \frac{V_0}{3} \right)^2 + \left(V_0 - \frac{2V_0}{3} \right)^2 \right\}$$
$$= \frac{1}{6} C V_0^2$$

PARAGRAPH 2

One twirls a circular ring (of mass M and radius R) near the tip of one's finger as shown in Figure 1. In the process the finger never loses contact with the inner rim of the ring. The finger traces out the surface of a cone, shown by the dotted line. The radius of the path traced out by the point where the ring and the finger is in contact is r. The finger rotates with an angular velocity ω_0 . The rotating ring *rolls without slipping* on the outside of a smaller circle described by the point where the ring and the finger is in contact (Figure 2). The coefficient of friction between the ring and the finger is μ and the acceleration due to gravity is g.



*Q.17 The total kinetic energy of the ring is

| [A] | $M\omega_0^2 R^2$ | [B] | $\frac{1}{2}\mathrm{M}\omega_{0}^{2}(\mathrm{R}-\mathrm{r})^{2}$ |
|-----|----------------------------------|-----|--|
| [C] | $M\omega_0^2 \left(R-r\right)^2$ | [D] | $\frac{3}{2}M\omega_0^2\big(R-r\big)^2$ |

Sol.

С

A

*Q.18 The minimum value of ω_0 below which the ring will drop down is

$$\begin{array}{ll} [A] & \sqrt{\frac{g}{\mu(R-r)}} \\ [C] & \sqrt{\frac{3g}{2\mu(R-r)}} \end{array} \end{array} \begin{array}{ll} [B] & \sqrt{\frac{2g}{\mu(R-r)}} \\ [D] & \sqrt{\frac{g}{2\mu(R-r)}} \end{array} \end{array}$$

Sol.

PART II: CHEMISTRY

SECTION 1 [Maximum Marks: 21]

- This section contains SEVEN questions •
- . Each question has FOUR options [A], [B], [C] and [D]. ONLY ONE of these four options is correct.
- For each question, darken the bubble corresponding to the correct option in the ORS •
- For each question, marks will be awarded in one of the following categories: Full Marks +3 If only the bubble corresponding to the correct option is darkened : 0 If none of the bubbles is darkened Zero Marks : Negative Marks : -1 In all other cases
- Q.19. Pure water freezes at 273 K and 1 bar. The addition of 34.5 g of ethanol to 500 g of water changes the freezing point of the solution. Use the freezing point depression constant of water as 2 K kg mol⁻¹. The figures shown below represent plots of vapour pressure (V.P.) versus temperature (T). [molecular weight of ethanol is 46 g mol⁻¹]

Among the following, the option representing change the freezing point is



$$Zn(s)|ZnSO_4(aq)||CuSO_4(aq)|Cu(s)$$

When the concentration of Zn^{2+} is 10 times the concentration of Cu^{2+} , the expression for ΔG (in J mol⁻¹) is [F is Faraday constant; R is gas constant; T is temperature; $E^0(cell) = 1.1 \text{ V}$] [A] 1.1 F [B] 2.303 RT – 2.2 F [C] 2.303 RT + 1.1 F [D] -2.2 F В

Sol.

Sol.

 $Zn - 2e \longrightarrow Zn^{2+}$ $Cu^{2+} + 2e \longrightarrow Cu$ $Zn + Cu^{2+} \longrightarrow Zn^{2+} + Cu$

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$$E_{cell} = E_{cell}^{o} - \frac{2.303RT}{nF} \log \frac{\left[Zn^{2+}\right]}{\left[Cu^{2+}\right]}$$
$$E_{cell} = 1.1 - \frac{2.303RT}{2F} \log 10$$
$$= 1.1 - \frac{2.303RT}{2F}$$
$$\Delta G = -nFE_{cell}$$
$$= -2F\left(1.1 - \frac{2.303RT}{2F}\right)$$
$$= 2.303RT - 2.2 F$$

*Q.21. The standard state Gibbs free energies of formation of C(graphite) and C(diamond) at T = 298 K are $\Delta_f G^0 \left[C(\text{graphite}) \right] = 0 \text{ kJmol}^{-1}$

$$\Delta_f G^0 \left[C(\text{diamond}) \right] = 2.9 \text{ kJmol}^{-1}$$

The standard state means that the pressure should be 1 bar, and substance should be pure at a given temperature. The conversion of graphite [C(graphite)] to diamond [C(diamond)] reduces its volume by 2×10^{-6} m³ mol⁻¹. If C(graphite) is converted to C(diamond) isothermally at T = 298 K, the pressure at which C(graphite) is in equilibrium with C(diamond), is [Useful information: $1 J = 1 \text{ kg m}^2\text{s}^{-2}$; $1 \text{ Pa} = 1 \text{ kg m}^{-1}\text{s}^{-2}$; $1 \text{ bar} = 10^5 \text{ Pa}$]

[A] 14501 bar [B] 58001 bar [C] 1450 bar [D] 29001 bar

Sol.

Α

 $\Delta G = PdV$ $\left[\Delta_{\rm f} {\rm G^{o}}_{\rm (diamond)} - \Delta_{\rm f} {\rm G^{o}}_{\rm (graphite)}\right] = {\rm PdV}$ 2.9×10^3 J mol⁻¹ = P × 2 × 10⁻⁶ m³ mol⁻¹ $P = 1.45 \times 10^9 Pa$ $P = 1.45 \times 10^9 \times 10^{-5}$ bar $P = 1.45 \times 10^4 \text{ bar}$ P = 14500 bar

Q.22. Which of the following combination will produce H_2 gas? [A] Fe metal and conc. HNO₃ [B] Cu metal and conc. HNO₃ [C] Zn metal and NaOH(aq) [D] Au metal and NaCN (aq) in the presence of air С

Sol.

*Q.23. The order of the oxidation state of the phosphorus atom in H_3PO_2 , H_3PO_4 , H_3PO_3 , and $H_4P_2O_6$ is [A] $H_3PO_3 > H_3PO_2 > H_3PO_4 > H_4P_2O_6$ [B] $H_3PO_4 > H_3PO_2 > H_3PO_3 > H_4P_2O_6$ [C] $H_3PO_4 > H_4P_2O_6 > H_3PO_3 > H_3PO_2$ [D] $H_3PO_2 > H_3PO_3 > H_4P_2O_6 > H_3PO_4$

Sol.

С

| Species | Oxidation state of P |
|--------------------------------|----------------------|
| H ₃ PO ₄ | +5 |
| $H_4P_2O_6$ | +4 |
| H_3PO_3 | +3 |
| H_3PO_2 | +1 |

 $Zn + 2NaOH \longrightarrow Na_2ZnO_2 + H_2 \uparrow$



| | SECTION 2 [Maximum Marks: 28] |
|---------------|---|
| • | This section contains SEVEN questions |
| • | Each question has FOUR options [A], [B], [C] and [D]. ONE OR MORE THAN ONE of these four option(s) is(are) correct |
| • | For each question, darken the bubble(s) corresponding to all the correct option(s) in the ORS |
| • | For each question, marks will be awarded in <u>one of the following categories:</u> |
| | <i>Full Marks</i> : +4 If only the bubble(s) corresponding to all the correct option(s) is (are) darkened |
| | <i>Partial Marks</i> : +1 For darkening a bubble corresponding to each correct option, provided NO incorrect option is darkened |
| | <i>Tero Marks</i> : 0 If none of the bubbles is darkened |
| | <i>Negative Marks</i> : -2 In all other cases |
| • | For example, if [A], [C] and [D] are all the correct options for a question, darkening all these three will get |
| | +4 marks; darkening only [A] and [D] will result in +2 marks; and darkening [A] and [B] will result in -2 marks, as a wrong option is also darkened |
| | marks, as a wrong option is also darkened. |
| Q.26. | The correct statement(s) about surface properties is(are) |
| | [A] Adsorption is accompanied by decrease in enthalpy and decrease in entropy of the system |
| | [B] The critical temperatures of ethane and nitrogen are 563 K and 126 K, respectively. The adsorption of activated charcoal at a given temperature |
| | [C] Cloud is an emulsion type of colloid in which liquid is dispersed phase and gas is dispersion medium |
| | [D] Brownian motion of colloidal particles does not depend on the size of the particles but depends on |
| C . 1 | viscosity of the solution |
| 501. | A, D In adsorption process both $\Delta H \& \Delta S$ is – ve. Higher the critical temperature of a gas higher the extent of |
| | adsorption. |
| | Cloud is not an emulsion. |
| | Brownian motion depends on the size of the particles. |
| *Q.27 | 7. For a reaction taking place in a container in equilibrium with its surroundings, the effect of temperature on |
| - | its equilibrium constant K in terms of change in entropy is described by |
| | [A] With increase in temperature, the value of K for exothermic reaction decreases because entropy change |
| | [B] With increase in temperature, the value of K for endothermic reaction increases because unfavourable |
| | change in entropy of the surroundings decreases |
| | [C] With increase in temperature, the value of K for endothermic reaction increases because the entropy |
| | change of the system is negative [D] With increase in temperature, the value of K for exothermic reaction decreases because favourable. |
| | change in entropy of the surrounding decreases |
| Sol. | B, D |
| | [B] With increase in temperature, the value of <i>K</i> for endothermic reaction increases because unfavourable |
| | change in entropy of the surroundings decreases $[D]$ With increase in temperature, the value of K for exothermic reaction decreases because favourable |
| | change in entropy of the surrounding decreases |
| | |
| 0.28 | In a bimolecular reaction, the steric factor P was experimentally determined to be 4.5. The correct option(s) |
| X .20. | among the following is(are) |
| | [A] The activation energy of the reaction is unaffected by the value of the steric factor |
| | [B] Experimentally determined value of frequency factor is higher than that predicted by Arrhenius |
| | [C] Since $P = 4.5$, the reaction will not proceed unless an effective catalyst is used |
| | [D] The value of frequency factor predicted by Arrhenius equation is higher than that determined |
| | experimentally |
| | |

Sol. A, B

- [A] The activation energy of the reaction is unaffected by the value of the steric factor
- [B] Experimentally determined value of frequency factor is higher than that predicted by Arrhenius equation
- Q.29. For the following compounds, the correct statement(s) with respect to nucleophilic substitution reactions is(are)



- [A] I and III follow S_N 1 mechanism
- [B] I and II follow $S_N 2$ mechanism
- [C] Compound IV undergoes inversion of configuration
- [D] The order of reactivity for I, III and IV is: IV > I > III

Sol. A, B, C, D

Benzylic and 3° halides both follow S_N1 mechanism. Benzylic and 1° halides both follow S_N2 mechanism. Benzylic 2° halides can undergo inversion of configuration. The order of reactivity would be IV > I > III if both S_N1 and S_N2 are considered suitably for substrates.

*Q.30. Among the following, the correct statement(s) is(are)

- [A] Al(CH₃)₃ has the three-centre two-electron bonds in its dimeric structure
- [B] BH₃ has the three-centre two-electron bonds in its dimeric structure
- [C] AlCl₃ has the three-centre two-electron bonds in its dimeric structure
- [D] The Lewis acidity of BCl₃ is greater than that of AlCl₃

Sol. A, B, D

Both Al(CH₃)₃ and BH₃ has 3c - 2e bonds in the dimeric structure. CH₃ CH₃ CH₃



BCl₃ is stronger Lewis acid than AlCl₃.

Q.31. The option(s) with only amphoteric oxides is(are) [A] Cr₂O₃, BeO, SnO, SnO₂ [C] NO, B₂O₃, PbO, SnO₂

[B] Cr₂O₃, CrO, SnO, PbO[D] ZnO, Al₂O₃, PbO, PbO₂

Sol. A, D

Amphoteric oxides are ZnO, Al₂O₃, PbO, PbO₂, BeO, SnO, SnO₂, Cr₂O₃ NO is a neutral oxide. CrO is a basic oxide. B₂O₃ is an acidic oxide Q.32. Compounds **P** and **R** upon ozonolysis produce **Q** and **S**, respectively. The molecular formula of **Q** and **S** is C_8H_8O . **Q** undergoes Cannizzaro reaction but not haloform reaction, whereas **S** undergoes haloform reaction but not Cannizzaro reaction.

(i)
$$\mathbf{P} \xrightarrow{i) O_3/CH_2Cl_2} \mathbf{Q}_{(C_8H_8O)}$$

(ii) $\mathbf{R} \xrightarrow{i) O_3/CH_2Cl_2} \mathbf{S}_{(C_8H_8O)}$

The option(s) with suitable combination of **P** and **R**, respectively, is(are)



Sol.



Undergoes Cannizzaro but not haloform



Undergoes Haloform but not Cannizzaro



Undergoes Cannizzaro but not haloform



Undergoes Haloform but not Cannizzaro

For (C) and (D) options no. of carbons are not matching

SECTION 3 (Maximum Marks: 12)

- This section contains **TWO** paragraphs
- Based on each paragraph, there will be **TWO** questions
- Each question has **FOUR** options [A], [B], [C] and [D]. **ONLY ONE** of these four options is correct
- For each question, darken the bubble(s) corresponding to the correct option in the ORS
- For each question, marks will be awarded in <u>one of the following categories</u>:
- Full Marks: +3 If only the bubble corresponding to all the correct option is darkenedZero Marks: 0 In all other cases.

PARAGRAPH 1

Upon heating KClO₃ in the presence of catalytic amount of MnO_2 , a gas W is formed. Excess amount of W reacts with white phosphorus to give X. The reaction of X with HNO₃ gives Y and Z.

Solution for the Q. No. 33 to 34

 $2\text{KClO}_{3} \xrightarrow{\text{MnO}_{2}} 2\text{KCl} + 3\text{O}_{2}$ $P_{4} + 5\text{O}_{2} \xrightarrow{\text{P}_{4}\text{O}_{10}} P_{4}\text{O}_{10}$ $P_{4}\text{O}_{10} + 4\text{HNO}_{3} \xrightarrow{\text{HPO}_{3}} + 2\text{N}_{2}\text{O}_{5}$

[B] O₂ and P₄O₆
[D] O₃ and P₄O₁₀

Q.33. C

Q.34. **B**

PARAGRAPH 2

The reaction of compound **P** with CH₃MgBr(excess) in $(C_2H_5)_2O$ followed by addition of H₂O gives **Q**. The compound **Q** on treatment with H₂SO₄ at 0°C gives **R**. The reaction of **R** with CH₃COCl in the presence of anhydrous AlCl₃ in CH₂Cl₂ followed by treatment with H₂O produces compound **S** [Et in compound **P** is ethyl group]



Q. 35 The product S is







- *Q. 36 The reactions, **Q** to **R** and **R** to **S**, are
 - [A] Dehydration and Friedel-Crafts acylation
 - [B] Aromatic sulfonation and Friedel-Crafts acylation
 - [C] Friedel-Crafts alkylation, dehydration and Friedel-Crafts acylation
 - [D] Friedel-Crafts alkylation and Friedel-Crafts acylation

Solution for the Q. No. 35 to 36



Q.35. A

Q.36. C

PART III: MATHEMATICS

SECTION 1 (Maximum Marks: 21)

- This section contains **SEVEN** questions.
- Each question has FOUR options [A], [B], [C] and [D]. ONLY ONE of these four options is correct.
- For each question, darken the bubble corresponding to the correct option in the ORS.
- For each question, marks will be awarded in <u>one of the following categories:</u> *Full Marks* : +3 If only the bubble corresponding to the correct option is darkened.

Zero Marks : 0 If none of the bubbles is darkened. Negative Marks : -1 In all other cases.

Q.37 The equation of the plane passing through the point (1, 1, 1) and perpendicular to the planes 2x + y - 2z = 5and 3x - 6y - 2z = 7, is [A] 14x + 2y - 15z = 1 [B] 14x - 2y + 15z = 27

Sol.

С

Let direction ratios of normal be $\,\vec{n}$

[C] 14x + 2y + 15z = 31

 $\Rightarrow \vec{n} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & 1 & -2 \\ 3 & -6 & -2 \end{vmatrix} = -14\hat{i} - 2\hat{j} - 15\hat{k}$

 $\Rightarrow \text{ equation of plane is}$ -14(x-1) - 2(y-1) - 15(z-1) = 0 $\Rightarrow 14x + 2y + 15z = 31$

Q.38 Let *O* be the origin and let *PQR* be an arbitrary triangle. The point *S* is such that $\overrightarrow{OP} \cdot \overrightarrow{OQ} + \overrightarrow{OR} \cdot \overrightarrow{OS} = \overrightarrow{OR} \cdot \overrightarrow{OP} + \overrightarrow{OQ} \cdot \overrightarrow{OS} = \overrightarrow{OQ} \cdot \overrightarrow{OR} + \overrightarrow{OP} \cdot \overrightarrow{OS}$

Then the triangle *PQR* has *S* as its [A] centroid [C] incentre

[B] circumcentre[D] orthocenter

[D] -14x + 2y + 15z = 3

Sol.

D

$$OP \cdot OQ + OR \cdot OS = OR \cdot OP + OQ \cdot OS$$

$$\Rightarrow \overrightarrow{OP} \cdot \left(\overrightarrow{OQ} - \overrightarrow{OR}\right) = \overrightarrow{OS} \cdot \left(\overrightarrow{OQ} - \overrightarrow{OR}\right)$$

$$\Rightarrow \left(\overrightarrow{OP} - \overrightarrow{OS}\right) \cdot \left(\overrightarrow{RQ}\right) = 0$$

$$\left(\overrightarrow{SP}\right) \cdot \left(\overrightarrow{RQ}\right) = 0$$

$$\Rightarrow \overrightarrow{SP} \perp \overrightarrow{RQ}$$

Similarly $\overrightarrow{SR} \perp \overrightarrow{QP}$ and $\overrightarrow{SQ} \perp \overrightarrow{PR}$
Hence, S is orthocentre

Q.39 If y = y(x) satisfies the differential equation

$$8\sqrt{x}\left(\sqrt{9+\sqrt{x}}\right)dy = \left(\sqrt{4+\sqrt{9+\sqrt{x}}}\right)^{-1}dx, \quad x > 0$$

and $y(0) = \sqrt{7}$, then $y(256) =$
[A] 3 [B] 9
[C] 16 [D] 80

Sol. A $dy = \left(\frac{1}{8\sqrt{x}\left(\sqrt{9+\sqrt{x}}\right)\left(\sqrt{4+\sqrt{9+\sqrt{x}}}\right)}\right) dx$ Let $4 + \sqrt{9+\sqrt{x}} = t$ $\Rightarrow \frac{1}{2\sqrt{9+\sqrt{x}}} \cdot \frac{1}{2\sqrt{x}} dx = dt$ $\Rightarrow dy = \frac{dt}{2\sqrt{t}}$ $\Rightarrow 2dy = \frac{1}{\sqrt{t}} dt$ $2y = 2\sqrt{t} + c$ $\Rightarrow 2y = 2\sqrt{4+\sqrt{9+\sqrt{x}}} + c$ $y(0) = \sqrt{7} \Rightarrow c = 0$ $y = \sqrt{4+\sqrt{9+\sqrt{x}}}$ y(256) = 3

Q.40 If $f: \mathbb{R} \to \mathbb{R}$ is a twice differentiable function such that f''(x) > 0 for all $x \in \mathbb{R}$, and $f\left(\frac{1}{2}\right) = \frac{1}{2}$, f(1) = 1, then

| $[\mathbf{A}]f'(1) \le 0$ | [B] $0 < f'(1) \le \frac{1}{2}$ |
|---------------------------------|---------------------------------|
| $[C] \frac{1}{2} < f'(1) \le 1$ | [D] $f'(1) > 1$ |

Sol.

D

Let h(x) = f(x) - x $h\left(\frac{1}{2}\right) = 0 = h(1)$ $\Rightarrow h'(\alpha) = 0$ for some $\alpha \in (0, 1)$ by rolle's theorem $f'(\alpha) = 1$ as $f''(x) > 0 \Rightarrow f'(x)$ is increasing $\therefore f'(1) > f'(\alpha)$ f'(1) > 1

Q.41 How many 3×3 matrices M with entries from $\{0, 1, 2\}$ are there, for which the sum of the diagonal entries of $M^{T}M$ is 5? [A] 126 [B] 198 [C] 162 [D] 135

Sol.

B

Let matrix M = [k_{ij}] Then sum of diagonal entries = $\sum k_{ij}^2$ $\Rightarrow \sum k_{ij}^2 = 5$ where k_{ij} are from {0, 1, 2} \Rightarrow Total number of matrices = ${}^{9}C_{5} + {}^{9}C_{1} \cdot {}^{8}C_{1} = 198$

Q.42 Let $S = \{1, 2, 3, \dots, 9\}$. For $k = 1, 2, \dots, 5$, let N_k be the number of subsets of S, each containing five elements out of which exactly k are odd. Then $N_1 + N_2 + N_3 + N_4 + N_5 =$ [A] 210 [B] 252 [C] 125 [D] 126

Sol. D

There are only 4 even numbers in S

- Any subset of 5 elements of S will have at least 1 odd number.
- $\Rightarrow \qquad N_1 + N_2 + N_3 + N_4 + N_5 = {}^9C_5 = 126$
- Q.43 Three randomly chosen nonnegative integers x, y and z are found to satisfy the equation x + y + z = 10. Then the probability that z is even, is

| [A] $\frac{36}{55}$ | [B] <u>6</u> 11 | |
|---------------------|----------------------------------|---|
| [C] $\frac{1}{2}$ | [D] ⁵ / ₁₁ | - |

Sol.

B

Total number of solutions = ${}^{10+3-1}C_{3-1} = 66$

Favourable number of solutions = ${}^{11}C_1 + {}^{9}C_1 + {}^{7}C_1 + {}^{5}C_1 + {}^{3}C_1 + {}^{1}C_1 = 36$

$$P(req) = \frac{36}{66} = \frac{6}{11}$$

SECTION 2 (Maximum Marks: 28)

• This section contains SEVEN questions.

20 0

- Each question has FOUR options [A], [B], [C] and [D]. ONE OR MORE THAN ONE of these four options is(are) correct.
- For each question, darken the bubble(s) corresponding to all the correct option(s) in the ORS.

| For each question, marks will be awarded in one of the following categories: | | | | | |
|---|---|-----|--|--|--|
| <i>Full Marks</i> : +4 If only the bubble(s) corresponding to all the correct option(s) is(are) darkened. | | | | | |
| Partial Marks | : | + 1 | For darkening a bubble corresponding to each correct option, provided NO | | |
| | | | incorrect option is darkened. | | |
| Zero Marks | : | 0 | If none of the bubbles is darkened. | | |
| Negative Marks | : | -2 | In all other cases. | | |

• For example, if [A], [C] and [D] are all the correct options for a question, darkening all these three will get +4 marks; darkening only [A] and [D] will get +2 marks; and darkening [A] and [B] will get -2 marks, as a wrong option is also darkened.

Q.44 If
$$g(x) = \int_{\sin x}^{\sin(2x)} \sin^{-1}(t) dt$$
, then
[A] $g'\left(\frac{\pi}{2}\right) = -2\pi$
[B] $g'\left(-\frac{\pi}{2}\right) = 2\pi$
[C] $g'\left(\frac{\pi}{2}\right) = 2\pi$
[D] $g'\left(-\frac{\pi}{2}\right) = -2\pi$

Sol. Bonus

$$g(x) = \int_{\sin x}^{\sin(2x)} \sin^{-1}(t) dt$$

g'(x) = 2 (cos 2x) sin⁻¹ (sin 2x) - (cos x) sin⁻¹(sin x)
g'($\frac{\pi}{2}$) = 2(-1)(0) - cos($\frac{\pi}{2}$)(1) = 0
g'($-\frac{\pi}{2}$) = 0 no option is matching.

* Q.45 Let α and β be nonzero real numbers such that $2(\cos\beta - \cos\alpha) + \cos\alpha \cos\beta = 1$. Then which of the following is/are true ?

[A]
$$\tan\left(\frac{\alpha}{2}\right) + \sqrt{3}\tan\left(\frac{\beta}{2}\right) = 0$$

[B] $\sqrt{3}\tan\left(\frac{\alpha}{2}\right) + \tan\left(\frac{\beta}{2}\right) = 0$
[C] $\tan\left(\frac{\alpha}{2}\right) - \sqrt{3}\tan\left(\frac{\beta}{2}\right) = 0$
[D] $\sqrt{3}\tan\left(\frac{\alpha}{2}\right) - \tan\left(\frac{\beta}{2}\right) = 0$

Sol.

A, C

 $\cos\beta (2 + \cos\alpha) = 1 + 2 \cos \alpha$ $\frac{\cos\beta}{1} = \frac{1 + 2 \cos \alpha}{2 + \cos \alpha}$ $\frac{\cos\beta + 1}{\cos\beta - 1} = \frac{3(\cos\alpha + 1)}{\cos\alpha - 1}$ $\frac{2\cos^2\frac{\beta}{2}}{-2\sin^2\frac{\beta}{2}} = \frac{3 \times 2\cos^2\frac{\alpha}{2}}{-2\sin^2\frac{\alpha}{2}}$ $\tan^2\frac{\alpha}{2} = 3\tan^2\frac{\beta}{2}$ $\Rightarrow \quad \tan\frac{\alpha}{2} = \pm\sqrt{3}\tan\frac{\beta}{2}.$

Q.46If $f: \mathbb{R} \to \mathbb{R}$ is a differentiable function such that f'(x) > 2f(x) for all $x \in \mathbb{R}$, and f(0) = 1, then
[A] f(x) is increasing in $(0, \infty)$ [B] f(x) is decreasing in $(0, \infty)$ $[C] f(x) > e^{2x}$ in $(0, \infty)$ $[D] f'(x) < e^{2x}$ in $(0, \infty)$

Sol. A, C

$$f'(x) - 2f(x) > 0$$

$$\Rightarrow \frac{d}{dx} (f(x) \cdot e^{-2x}) > 0$$

$$\Rightarrow f(x) \cdot e^{-2x} \text{ is increasing function}$$

$$\Rightarrow f(x) \cdot e^{-2x} > f(0) = 1 \quad \forall x > 0$$

$$f(x) > e^{2x} \quad \forall x > 0$$

$$\Rightarrow f'(x) > 2f(x) > 2e^{2x} > 0 \quad \forall x > 0.$$
Q.47 Let $f(x) = \frac{1 - x(1 + |1 - x|)}{|1 - x|} \cos\left(\frac{1}{1 - x}\right) \text{ for } x \neq 1.$ Then
[A] $\lim_{x \to \Gamma} f(x) = 0$
[B] $\lim_{x \to \Gamma} f(x)$ does not exist
[C] $\lim_{x \to \Gamma^{+}} f(x) = 0$
[D] $\lim_{x \to \Gamma^{+}} f(x)$ does not exist

Sol. A, D $\lim_{x \to l^{-}} f\left(x\right) = \lim_{h \to 0} \frac{h^{2}}{h} \cos \frac{1}{h} = 0$ $\lim_{x \to 1^{+}} f(x) = \lim_{h \to 0} \frac{-h(2+h)}{h} \cos \frac{1}{h} \text{ does not exist}$ If $f(x) = \begin{vmatrix} \cos(2x) & \cos(2x) & \sin(2x) \\ -\cos x & \cos x & -\sin x \\ \sin x & \sin x & \cos x \end{vmatrix}$, then Q.48 [A] f'(x) = 0 at exactly three points in $(-\pi, \pi)$ [C] f(x) attains its maximum at x = 0B, C Żх

[B] f'(x) = 0 at more than three points in $(-\pi, \pi)$ [D] f(x) attains its minimum at x = 0

Sol.

$$f(x) = \begin{vmatrix} \cos 2x & \cos 2x & \sin 2x \\ -\cos x & \cos x & -\sin x \\ \sin x & \sin x & \cos x \end{vmatrix} = \cos 4x + \cos 2$$

Now $f'(x) = -2\sin 2x - 4\sin 4x = 0$
 $\Rightarrow f'(x) = 2\sin 2x (1 + 4\cos 2x) = 0$
Then $\sin 2x = 0$ or $\cos 2x = -\frac{1}{4}$
For $\sin 2x = 0$; $x = 0, \pi/2 - \pi/2$
For $\cos 2x = -1/4$ there are four solutions.
 $f'(x) = 0$ has more than three solutions.
Again $f''(x) = -(4\cos 2x + 16\cos 4x)$
 $\Rightarrow f''(0) < 0$

If the line $x = \alpha$ divides the area of region $R = \{(x, y) \in \mathbb{R}^2 : x^3 \le y \le x, 0 \le x \le 1\}$ into two equal parts, then Q.49 $[B] \ \frac{1}{2} < \alpha < 1$ [A] $0 < \alpha \le \frac{1}{2}$ [D] $\alpha^4 + 4\alpha^2 - 1 = 0$ $[C] 2\alpha^4 - 4\alpha^2 + 1 = 0$

B, C

$$\frac{1}{2} \left(\int_{0}^{1} \left(x - x^{3} \right) dx \right) = \int_{0}^{\alpha} \left(x - x^{3} \right) dx$$
$$\frac{1}{8} = \left| \frac{x^{2}}{2} - \frac{x^{4}}{4} \right|_{0}^{\alpha}$$
$$\frac{1}{2} = 2\alpha^{2} - \alpha^{4}$$
$$2\alpha^{4} - 4\alpha^{2} + 1 = 0$$
$$f(\alpha) = 2\alpha^{4} - 4\alpha^{2} + 1$$



Q.50 If
$$I = \sum_{k=1}^{98} \int_{k}^{k+1} \frac{k+1}{x(x+1)} dx$$
, then
[A] $I > \log_e 99$ [B] $I < \log_e 99$
[C] $I < \frac{49}{50}$ [D] $I > \frac{49}{50}$

Sol.

B, D

$$\begin{split} &\sum_{k=1}^{98} \int_{k}^{k+1} \frac{1}{x+1} \, dx < \sum_{k=1}^{98} \int_{k}^{k+1} \frac{k+1}{x(x+1)} \, dx < \sum_{k=1}^{98} \int_{k}^{k+1} \frac{dx}{x} \\ &\sum_{k=1}^{98} \Big(\ell n \left(k+2 \right) - \ell n \left(k+1 \right) \Big) < I < \sum_{k=1}^{98} \Big(\ell n \left(k+1 \right) - \ell nk \Big) \\ &\ell n \ 50 < I < \ell n \ 99 \\ \Rightarrow \quad \frac{49}{50} < I < \ell n 99 \ . \end{split}$$

SECTION 3 (Maximum Marks: 12)

- This section contains **TWO** paragraphs.
- Based on each paragraph, there are **TWO** questions.
- Each question has FOUR options [A], [B], [C] and [D]. ONLY ONE of these four options is correct.
- For each question, darken the bubble corresponding to the correct option in the ORS.
- For each question, marks will be awarded in <u>one of the following categories:</u> *Full Marks* : + 3 If only the bubble corresponding to the correct option is darkened. *Zero Marks* : 0 In all other cases.

PARAGRAPH 1

Let O be the origin, and \overrightarrow{OX} , \overrightarrow{OY} , \overrightarrow{OZ} be three unit vectors in the directions of the sides \overrightarrow{QR} , \overrightarrow{RP} , \overrightarrow{PQ} , respectively, of a triangle PQR.

Q.51 $|\overrightarrow{OX} \times \overrightarrow{OY}| =$ [A] sin(P + Q) [C] sin(P + R)

A

[B] $\sin 2R$ [D] $\sin(Q+R)$

Sol.



Q.52 If the triangle *PQR* varies, then the minimum value of



Let *p*, *q* be integers and let α , β be the roots of the equation, $x^2 - x - 1 = 0$, where $\alpha \neq \beta$. For n = 0, 1, 2, ..., let $a_n = p\alpha^n + q\beta^n$.

FACT : If *a* and *b* are rational numbers and $a + b\sqrt{5} = 0$, then a = 0 = b.

| * Q.53 | $a_{12} =$ [A] $a_{11} - a_{10}$ [C] $2a_{11} + a_{10}$ | [B] $a_{11} + a_{10}$ [D] $a_{11} + 2a_{10}$ |
|--------|---|---|
| Sol. | B As $a_{n+1}-a_n - a_{n-1} = 0$ So $a_{12} = a_{11} + a_{10}$ | |
| * Q.54 | If $a_4 = 28$, then $p + 2q =$ [A] 21 [C] 7 | [B] 14 [D] 12 |
| Sol. | $ \begin{array}{l} \textbf{D} \\ a_4 = 2a_0 + 3a_1 \\ a_4 = (q-p) \; (3\beta) + 5p + 2q = 28 \\ \Rightarrow p = q = 4. \end{array} $ | |

P2-17-6-1 PAPER-2 CODE [1]

BACK COVER PAGE IS AS PER THE ACTUAL PAPER

QUESTION PAPER FORMAT AND MARKING SCHEME

20. The question paper has three parts: Physics, Chemistry and Mathematics.

21. Each part has three sections as detailed in the following table:

| Section | Question Type | Number of Questions | Category-wise Marks for Each Question | | | | Maximum |
|---------|--|------------------------|--|---|---|---|-------------------------|
| | | | Full Marks | Partial Marks | Zero Marks | Negative Marks | Marks of the Section |
| 1 | Single Correct Option | 7 | +3 If only the bubble corresponding to the correct option is darkened | _ | 0 If none of the bubbles is darkened | – 1 In all other cases | 21 |
| 2 | One or more correct option(s) | 7 | +4 If only the bubble(s) corresponding to all the correct option(s) is(are) darkened | +1 For darkening a bubble corresponding to each correct option, provided NO incorrect option is darkened | 0 If none of the bubbles is darkened | - 2 In all other cases | 28 |
| 3 | Comprehe nsion | 4 | +3 If only the bubble corresponding to the correct option is darkened | _ | 0 In all other cases | _ | 12 |

NAME OF THE CANDIDATE

ROLL NO

| I have read all the instructions and shall abide by them. | I have verified the identify, name and roll number of the candidate, and that question paper and ORS codes are the same. |
|--|--|
| Signature of the Candidate | Signature of the Invigilator |

**1

36/36